

Heavy Flavor Spectroscopy on the Lattice

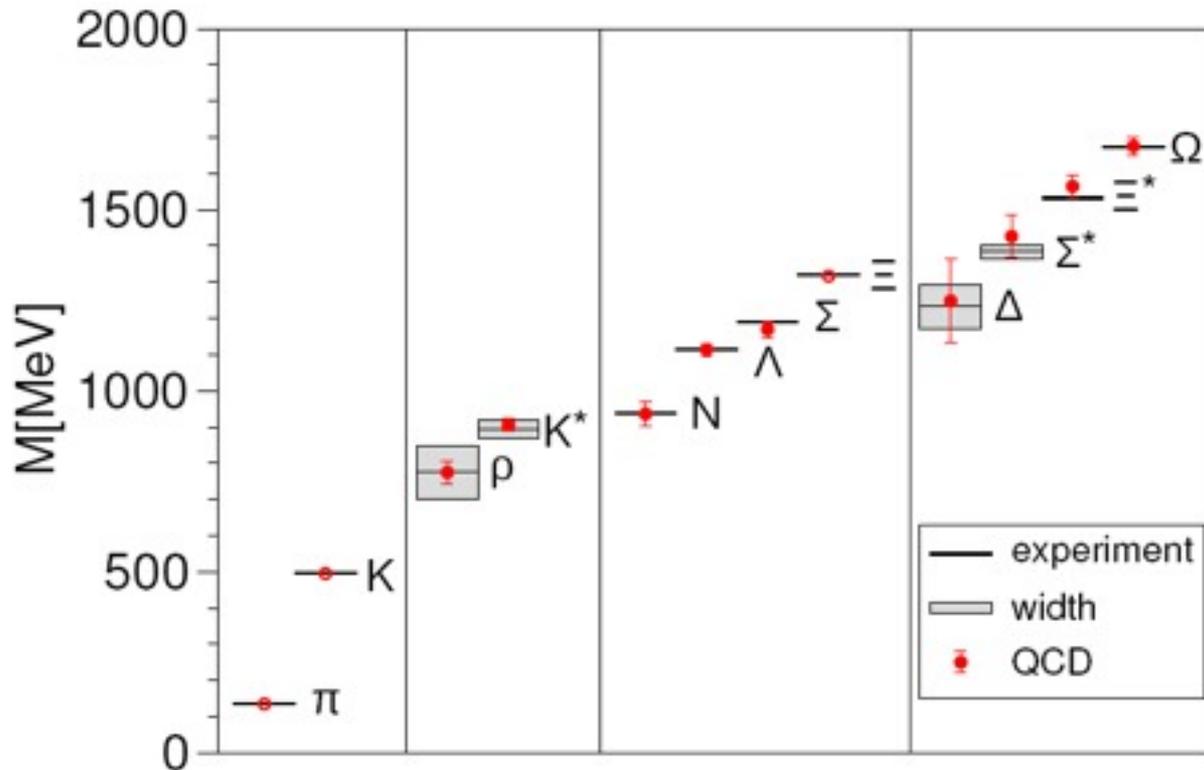
David Richards
Jefferson Laboratory

Lattice QCD Meets Experiment
FNAL
April 26-27, 2010

- Why are we interested?
- Renaissance in lattice spectroscopy
 - *Charmonium, and the new states....*
 - *Charmed and Bottom baryons*
 - *Future light-quark programs*
- Future prospects

Low-lying Hadron Spectrum

$$\begin{aligned}
 C(t) &= \sum_{\vec{x}} \langle 0 | N(\vec{x}, t) \bar{N}(0) | 0 \rangle = \sum_{n, \vec{x}} \langle 0 | e^{ip \cdot x} N(0) e^{-ip \cdot x} | n \rangle \langle n | \bar{N}(0) | 0 \rangle \\
 &= |\langle n | N(0) | 0 \rangle|^2 e^{-E_n t} = \sum_n A_n e^{-E_n t}
 \end{aligned}$$



Durr et al., BMW Collaboration

Science 2008

Control over:

- **Quark-mass dependence**
- **Continuum extrapolation**
- **finite-volume effects (pions, resonances)**

Benchmark calculation of QCD - *enabling us to do something else!*

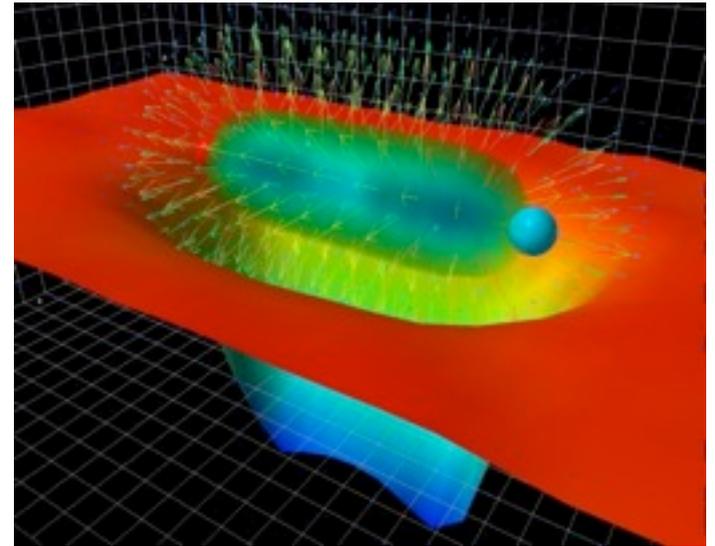
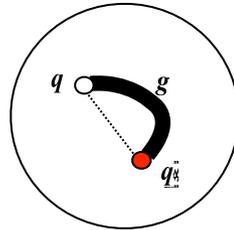
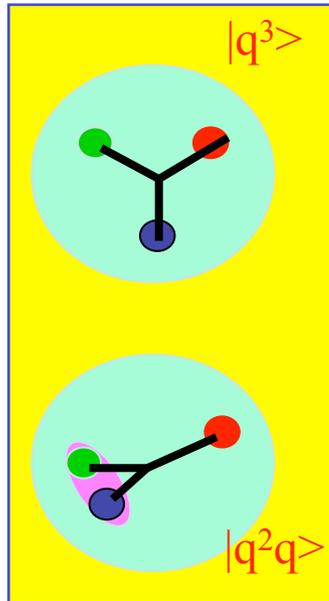
Goals - I

.....but a quantitative understanding of the spectrum is important *in its own right...*

- *Why is it important?*

- *What are the key degrees of freedom describing the bound states?*
 - *How do they change as we vary the quark mass?*
- *What is the role of the gluon in the spectrum – search for exotics?*
- *What is the origin of confinement, describing 99% of observed matter?*
- *If QCD is correct and we understand it, expt. data must confront ab initio calculations*

Goals - II



- Are states **Missing**, because our pictures do not capture correct degrees of freedom?
- Do they just not couple to **probes**?

- Exotic Mesons are those whose values of J^{PC} are in accessible to quark model
 - Multi-quark states:
 - Hybrids with *excitations of the flux-tube*
- Study of hybrids: revealing **gluonic** and **flux-tube** degrees of freedom of QCD.

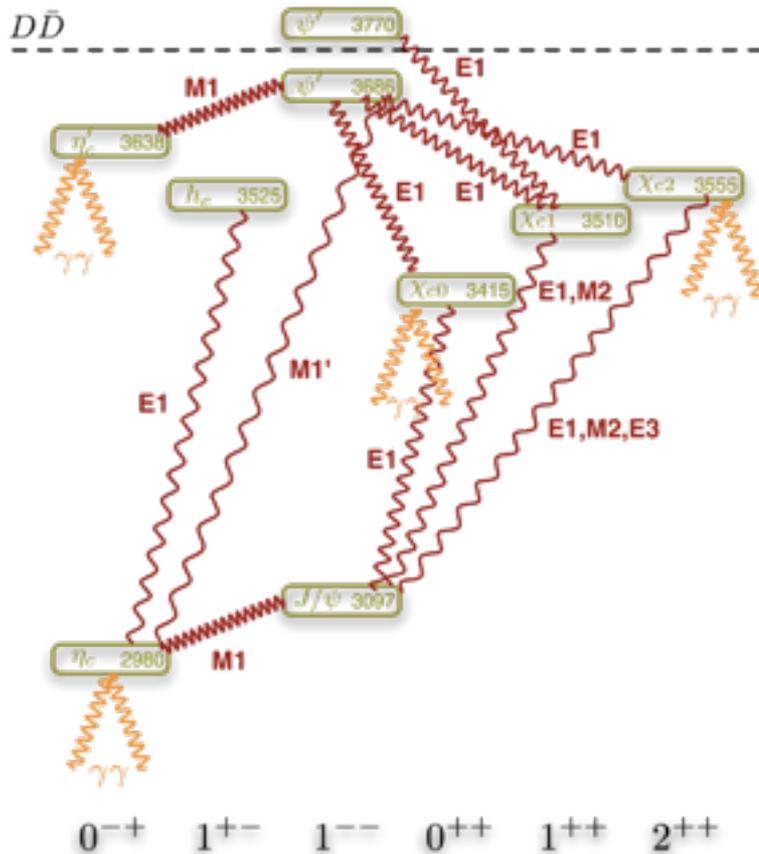
Variational Method

- Extracting excited-state energies described in C. Michael, NPB 259, 58 (1985) and Luscher and Wolff, NPB 339, 222 (1990)
- Can be viewed as exploiting the *variational method*
- Given $N \times N$ correlator matrix $C_{\alpha\beta} = \langle 0 | \mathcal{O}_\alpha(t) \mathcal{O}_\beta(0) | 0 \rangle$, one defines the N *principal correlators* $\lambda_i(t, t_0)$ as the eigenvalues of
$$C^{-1/2}(t_0)C(t)C^{-1/2}(t_0)$$
- Principal effective masses defined from correlators plateau to lowest-lying energies

$$\lambda_i(t, t_0) \rightarrow e^{-E_i(t-t_0)} \left(1 + O(e^{-\Delta E(t-t_0)}) \right)$$

Eigenvectors, with metric $C(t_0)$, are orthonormal and project onto the respective states

Charmonium



Plethora of states - *below the $D\bar{D}$ threshold*

Precision LQCD - testing *both QCD and our computational framework.*

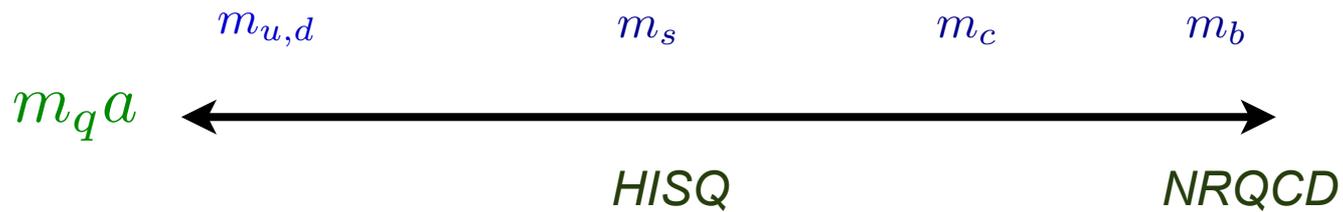
Challenges:

- *Discretisation uncertainties*
- *Precise inclusion of effects of light-quark degrees of freedom.*

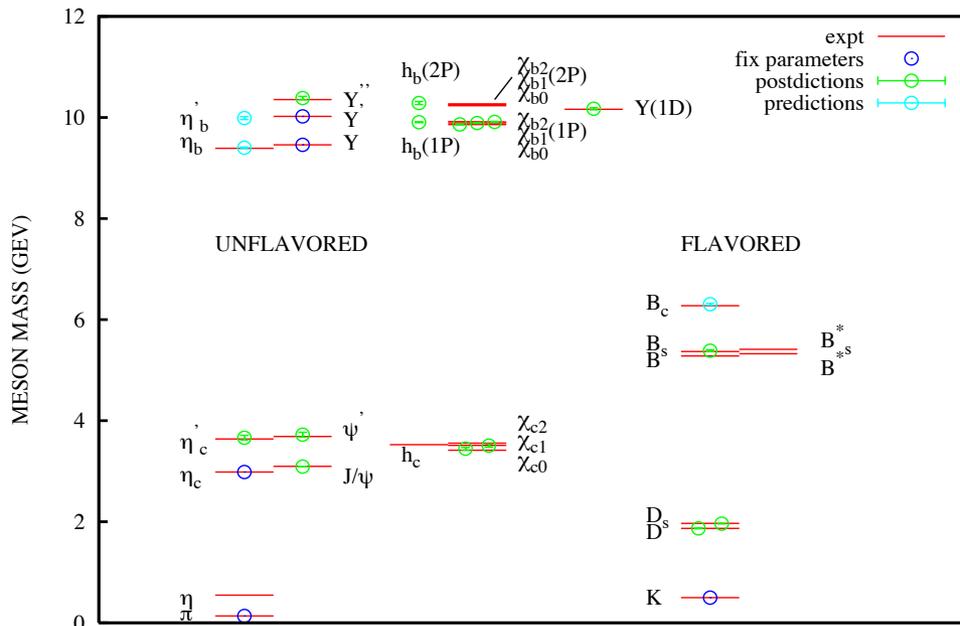
Approaches:

- *NRQCD*
- *Redefinition of action (FNAL)*
- *HISQ*

Charmonium - II



The gold-plated meson spectrum from lattice QCD - HPQCD 2008



Gold-plated observables -
HPQCD, arXiv:0810.3548

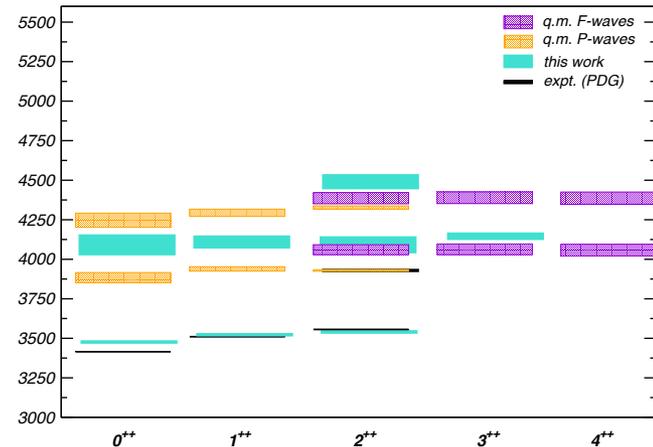
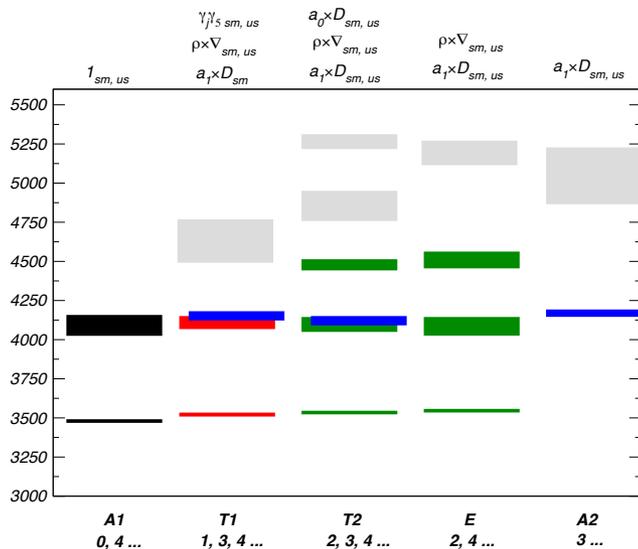
Charmonium - III

- Can we reliably compute higher states in spectrum?
- Can we reliably specify continuum quantum numbers?

*Dudek, Edwards, Mathur,
DGR, PRD78:094504
(08)*

$$C_{ij}(t) = \sum_{\vec{x}} \langle O_i(\vec{x}, t) O_j(\vec{0}, 0) \rangle = \sum_N \frac{Z_i^{(N)} Z_j^{(N)*}}{2m_N} e^{-m_N t}$$

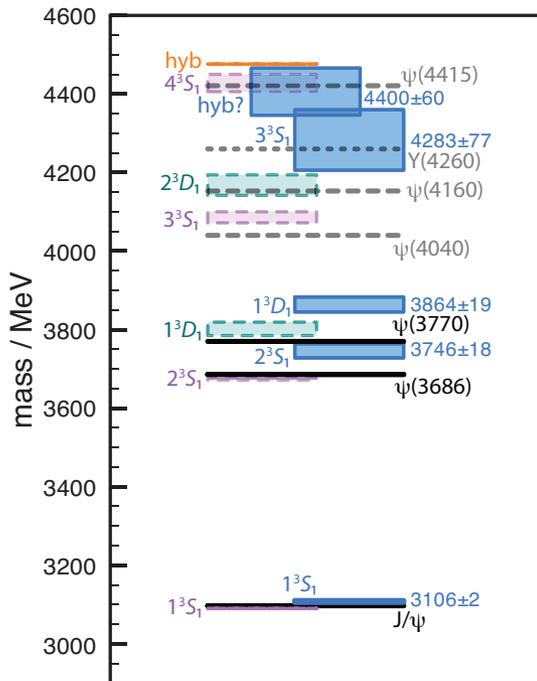
$Z_j^{(N)} \equiv \langle 0 | O_j | N \rangle$ contains information about quantum numbers of state



LQCD-based Phenomenology

What can we learn about the nature of the QCD spectrum, and the effective degrees of freedom of QCD?

Dudek and Rrapaj, PRD78:094504 (2008)



operator name	continuum limit	allowed J^{PC}	kinematic factor	quark model state	$f(q)$	origin behaviour
$a_0 \times \nabla$	$\bar{\psi} \partial^i \psi$	1^{--}	$MZ \in^i$	3S_1	$\frac{2\sqrt{2}}{3M} \frac{q^2}{m_q}$	$R_S''(0)$
$a_{0(2)} \times \nabla$	$\bar{\psi} \gamma^0 \partial^i \psi$	1^{-+}	$MZ \in^i$	3D_1	$\frac{4}{3M} \frac{q^2}{m_q}$	$R_D''(0)$
$\pi \times \nabla$	$\bar{\psi} \gamma^5 \partial^i \psi$	1^{+-}	$MZ \in^i$	exotic	0	0
$\pi(2) \times \nabla$	$\bar{\psi} \gamma^0 \gamma^5 \partial^i \psi$	1^{+-}	$MZ \in^i$	1P_1	$\frac{4\sqrt{2}}{\sqrt{3}M} q \left(1 + \frac{q^2}{4m_q^2}\right)$	$R_P'(0)$
$\rho \times \nabla$	$\bar{\psi} \gamma^i \partial^j \psi$	0^{++}	$MZ \delta^{ij}$	1P_1	$\frac{4\sqrt{2}}{\sqrt{3}M} q \left(1 - \frac{q^2}{4m_q^2}\right)$	$R_P'(0)$
		1^{++}	$MZ \epsilon^{ijk} \frac{q^k}{m_q}$	3P_0	$\frac{4\sqrt{2}}{3M} q \left(1 - \frac{q^2}{4m_q^2}\right)$	$R_P'(0)$
		2^{++}	$MZ \in^{ij}$	3P_1	$\frac{4}{\sqrt{3}M} q \left(1 + \frac{q^2}{4m_q^2}\right)$	$R_P'(0)$
				3P_2	$\frac{4\sqrt{2}}{\sqrt{3}M} q \left(1 + \frac{q^2}{20m_q^2}\right)$	$R_P'(0)$
				3F_2	$\frac{4}{5M} \frac{q^3}{m_q^2}$	$R_F'''(0)$

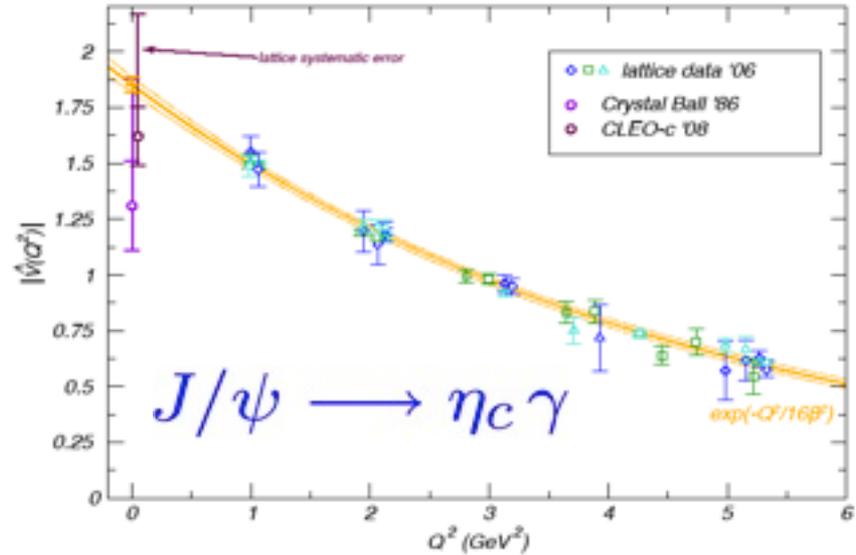
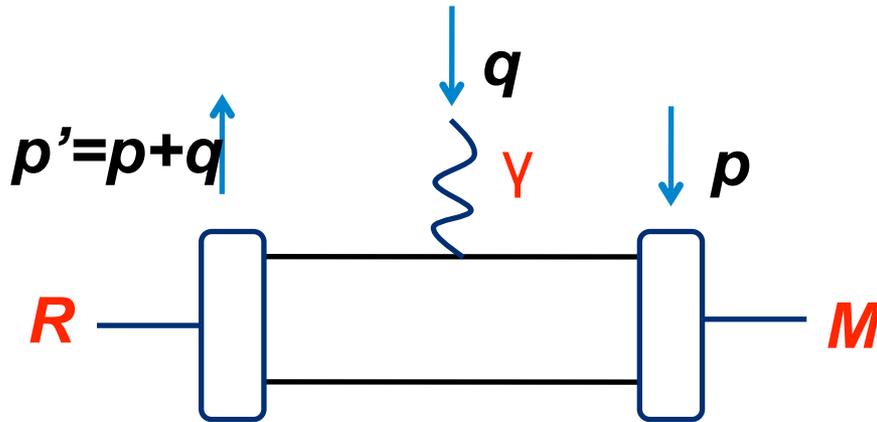
Phenomenological interpretation
Comparison with non-relativistic quark model

operator	0 th [4305(40)]	1 st [4645(86)]	2 nd [4689(138)]	3 rd [5580(160)]
$a_{0(2)} \times \nabla_{T1}^{(sm)} (10^{-3})$	2.5(2)	2.0(6)	2.0(7)	0.8(4)
$b_1 \times \nabla_{T1}^{(sm)} (10^{-3})$	2.2(2)	2.9(4)	1.7(8)	1.4(7)
$\rho \times \mathbb{B}_{T1}^{(sm)} (10^{-3})$	2.88(5)	0.2(2)	0.8(5)	0(0.3)
$\rho_2 \times \mathbb{B}_{T1}^{(sm)} (10^{-3})$	2.84(5)	0.0(2)	0.8(5)	0(0.3)
$a_{0(2)} \times \nabla_{T1} (10^{-3})$	1.8(1)	0.2(3)	1.2(5)	1.5(7)
$b_1 \times \nabla_{T1} (10^{-3})$	1.7(1)	0.2(4)	1.0(5)	0.8(11)
$\rho \times \mathbb{B}_{T1} (10^{-3})$	3.1(2)	0.4(7)	2.6(9)	3.6(20)
$\rho_2 \times \mathbb{B}_{T1} (10^{-3})$	3.0(2)	0.2(6)	2.5(9)	3.5(20)
assignment	1^{-+} hyb ?	$4^{-+} (^1G_4)$?	?	?

Radiative Transitions - I

Electro-magnetic properties - probe of EM structure

Dudek, Edwards, Richards, PRD73, 074507



$c\bar{c} \rightarrow \gamma\gamma$: Dudek, Edwards, PRL97, 172001 (2006).

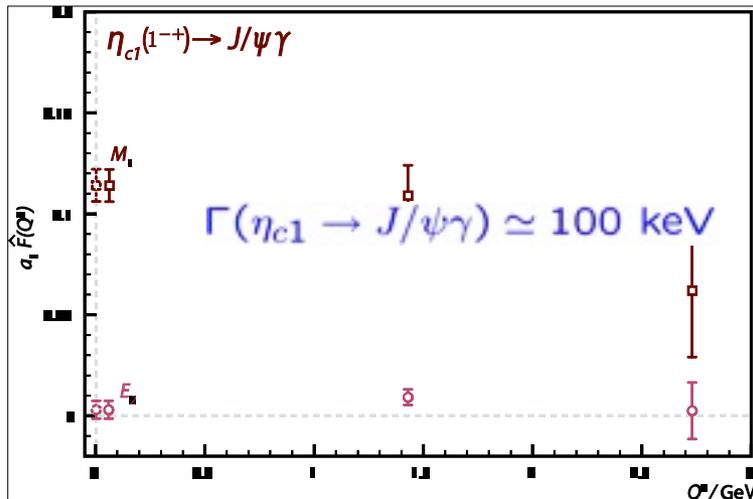
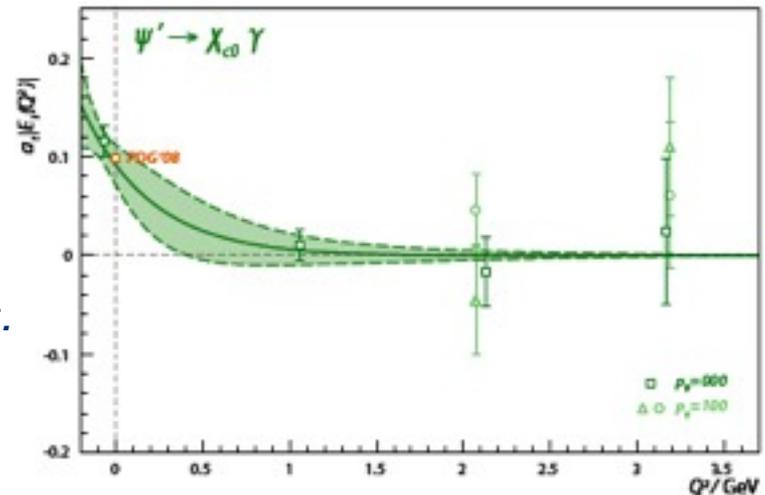
[hep-ex/0805.252](https://arxiv.org/abs/hep-ex/0805.252)

Experimental analysis by CLEO-c driven by lattice calculations

Spectrum and Properties of Mesons in LQCD

J Dudek, R Edwards, C Thomas, Phys. Rev. D79:094504 (2009).

Use of variational method, and the optimized meson operators, to compute *radiative transitions between excited states and exotics*.

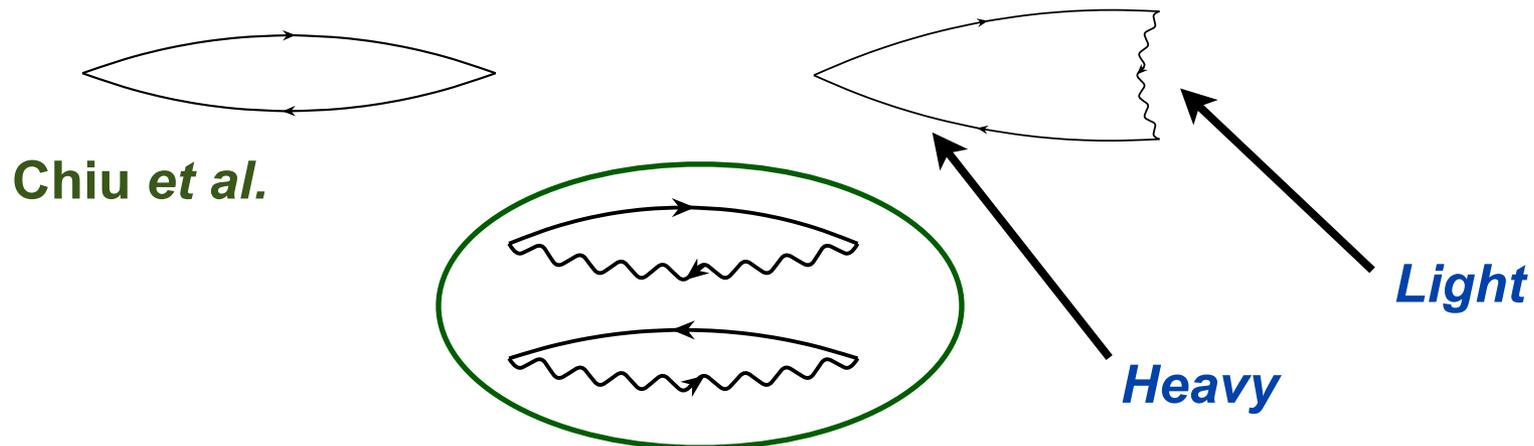


considerable phenomenology developed from the results - supports non-relativistic models and limits possibilities for form of excited glue

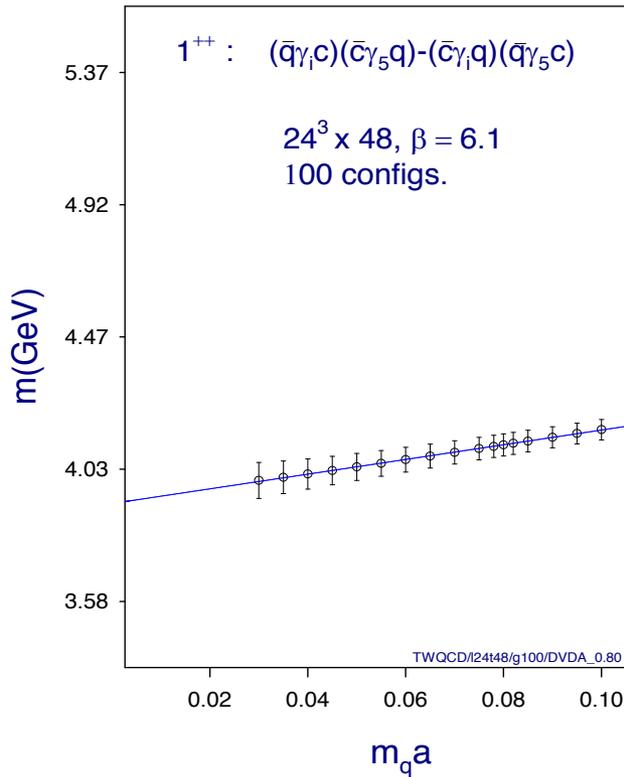
Radiative width of hybrid comparable to conventional meson

X, Y, Z...

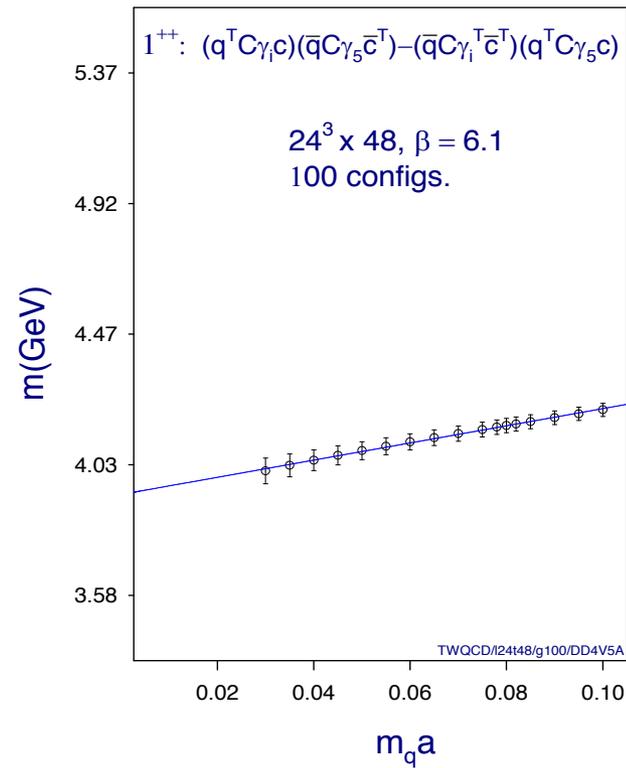
- Zoo of new States X(3872), Y(4260), Y(4140)
- X(3872) seen in many experiments both *B and proton-antiproton* - preferred quantum numbers $J^{PC}=1^{++}$.
- X is the candidate molecular or tetraquark state
- Can it be seen in lattice QCD?
 - Quantum numbers alone cannot eliminate simple charmonium state
 - Need to search for $\bar{c}q cq$
 - Such states have same quantum numbers as both charmonium, and indeed DD* in S-wave; we should see these states in the lattice spectrum



X,Y,Z,... II



“molecular”



Diquark-antidiquark

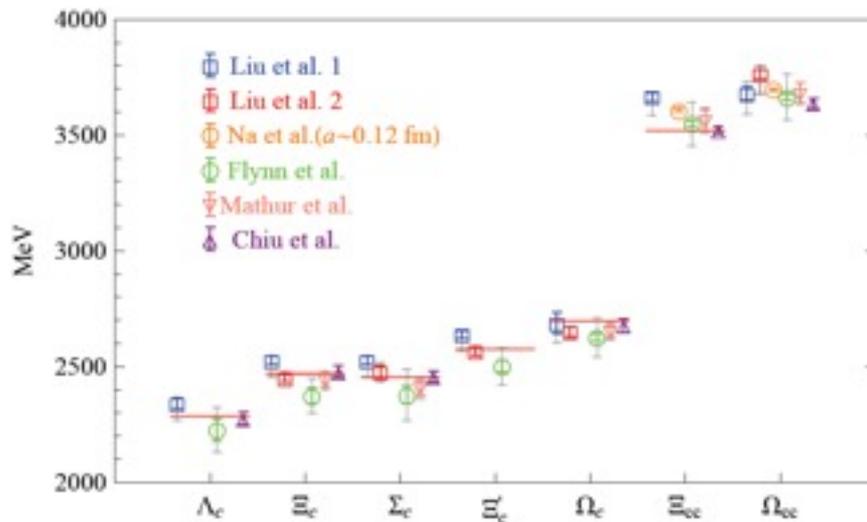
- *Quenched calculation...*
- *See molecular/tetraquark consistent with X(3872)*
- *But should also see the D + D* in an S-Wave*

Charmed and Bottom Baryons

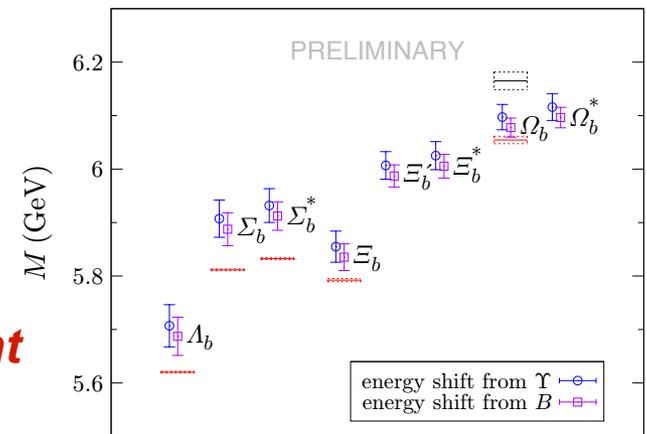
- SELEX, D0, CDF,... charmed and bottom baryons
- Recent calculation in full QCD: Asqtad for sea quarks, DWF for light quarks, FNAL Action for heavy quarks.

Use charmonium system to fix action

L. Liu et al, arXiv:0909.3294



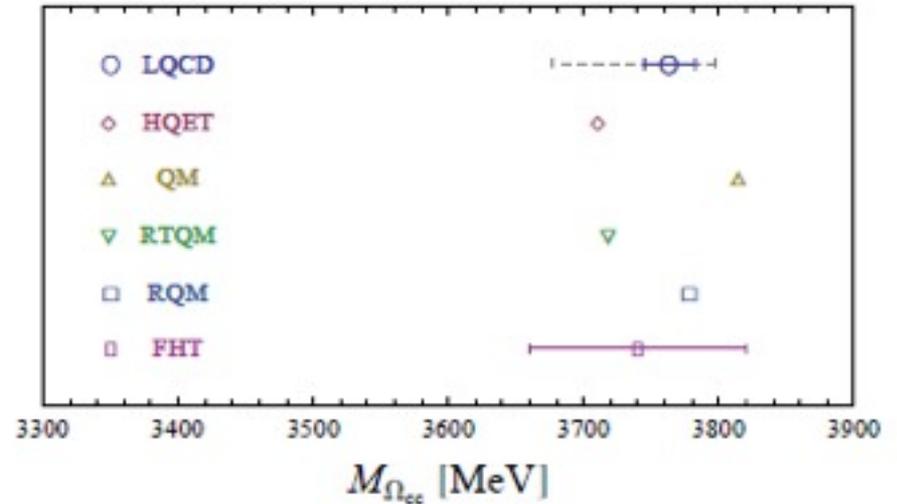
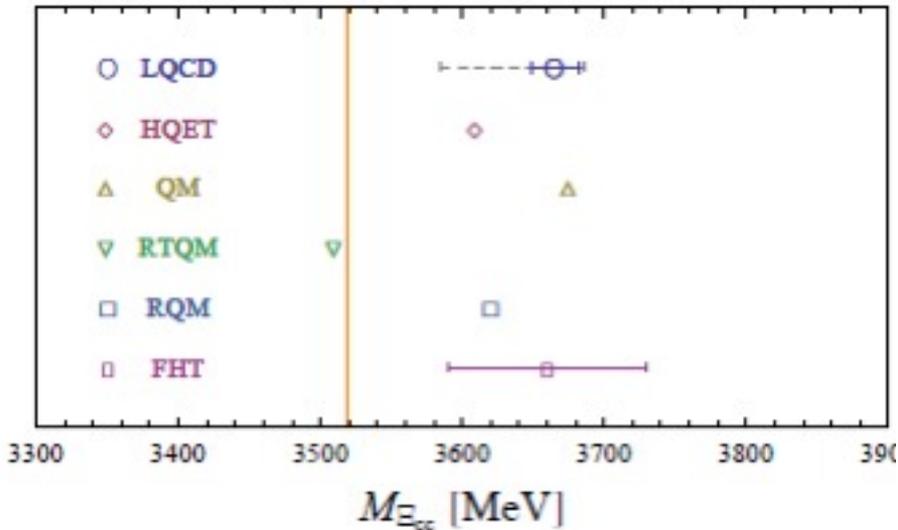
Meinel et al., arXiv:0909.3837



Experiment

DWF for light quarks

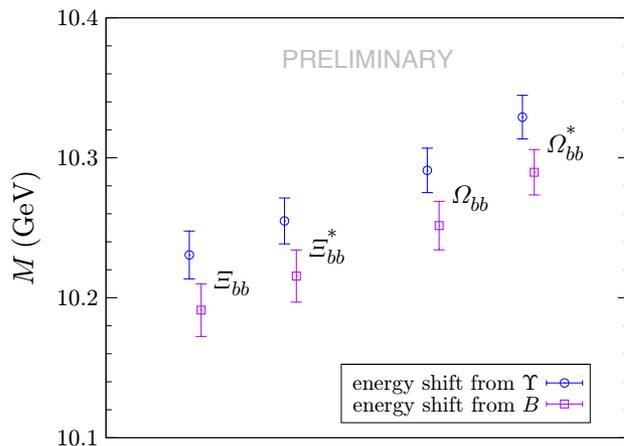
Doubly-charmed Baryons



Prediction: $M_{\Omega_{cc}} = 3763 \pm 19 \pm 26(+13 - 79)$ MeV

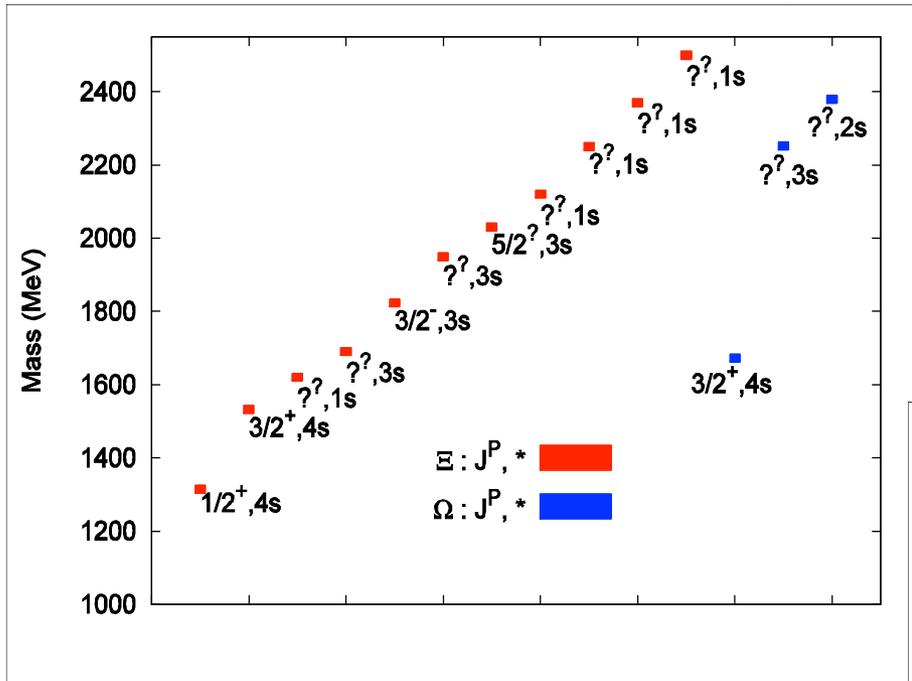
$$M_{\Omega_{bbb}} = 14.3748(33) \text{ GeV}$$

Inensitive to light dof?

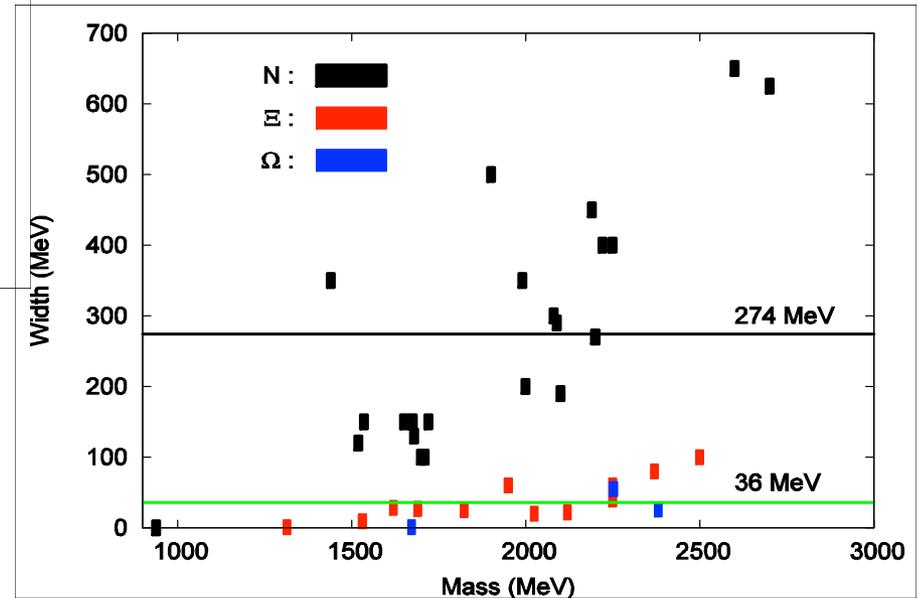


Discovery: cascade physics

Cascades (uss) are largely *terra incognita*



Thanks to N. Mathur



Light-Quark Physics

Goals- III

CLAS

baryon resonance

baryon spectrum

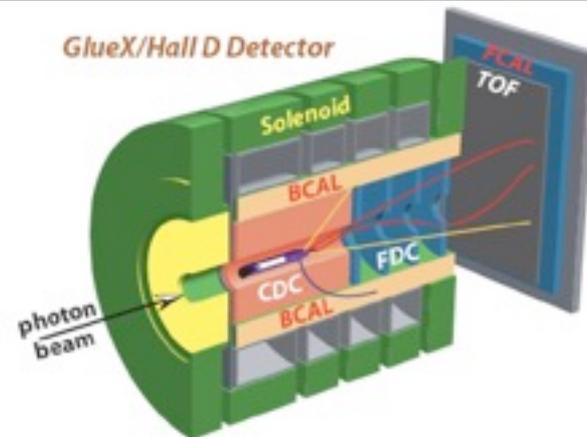
transition form-factors $N \xrightarrow{\gamma^*} N^*$

GlueX

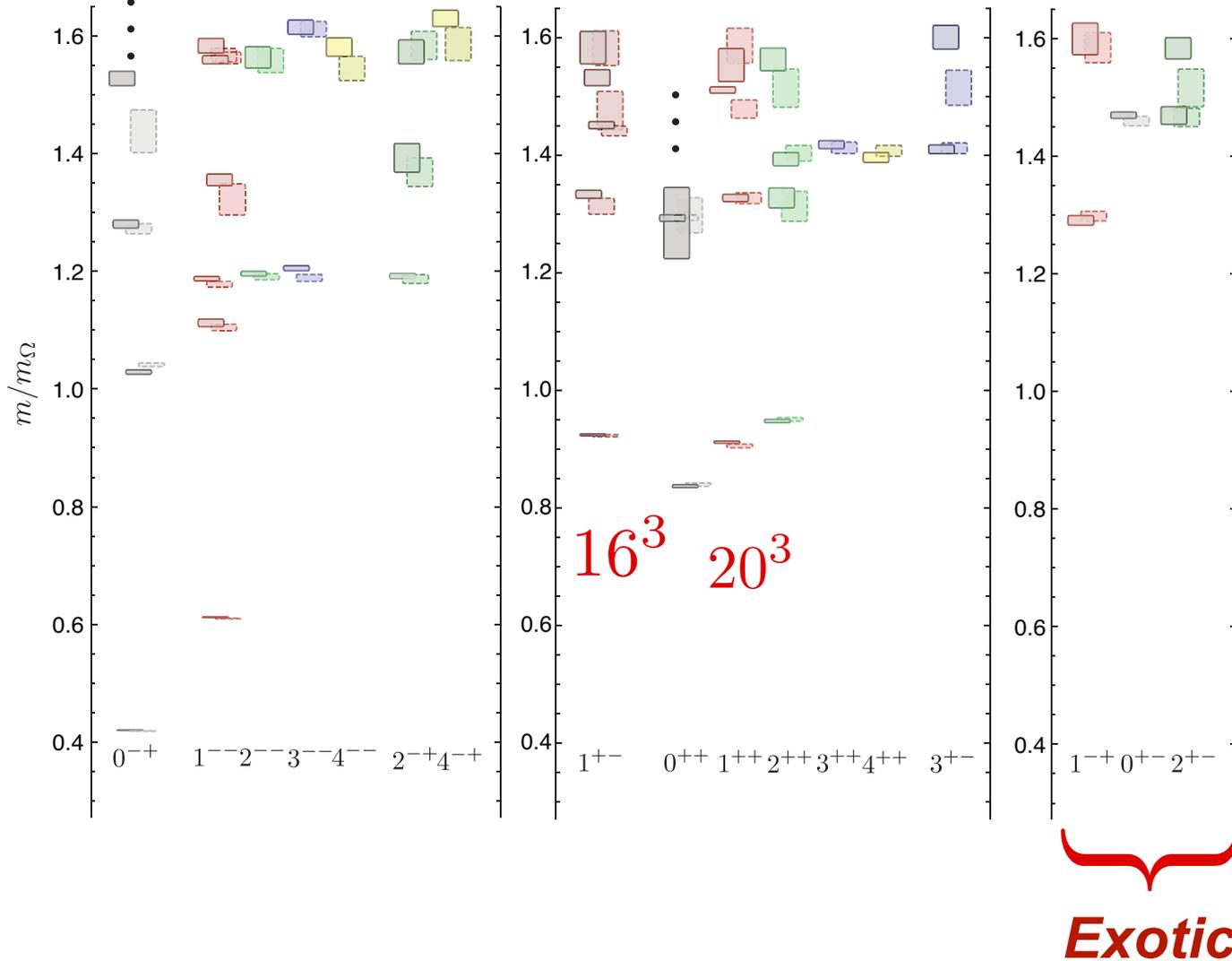
meson resonance

meson spectrum

photocouplings $g(m \xrightarrow{\gamma} m^*)$



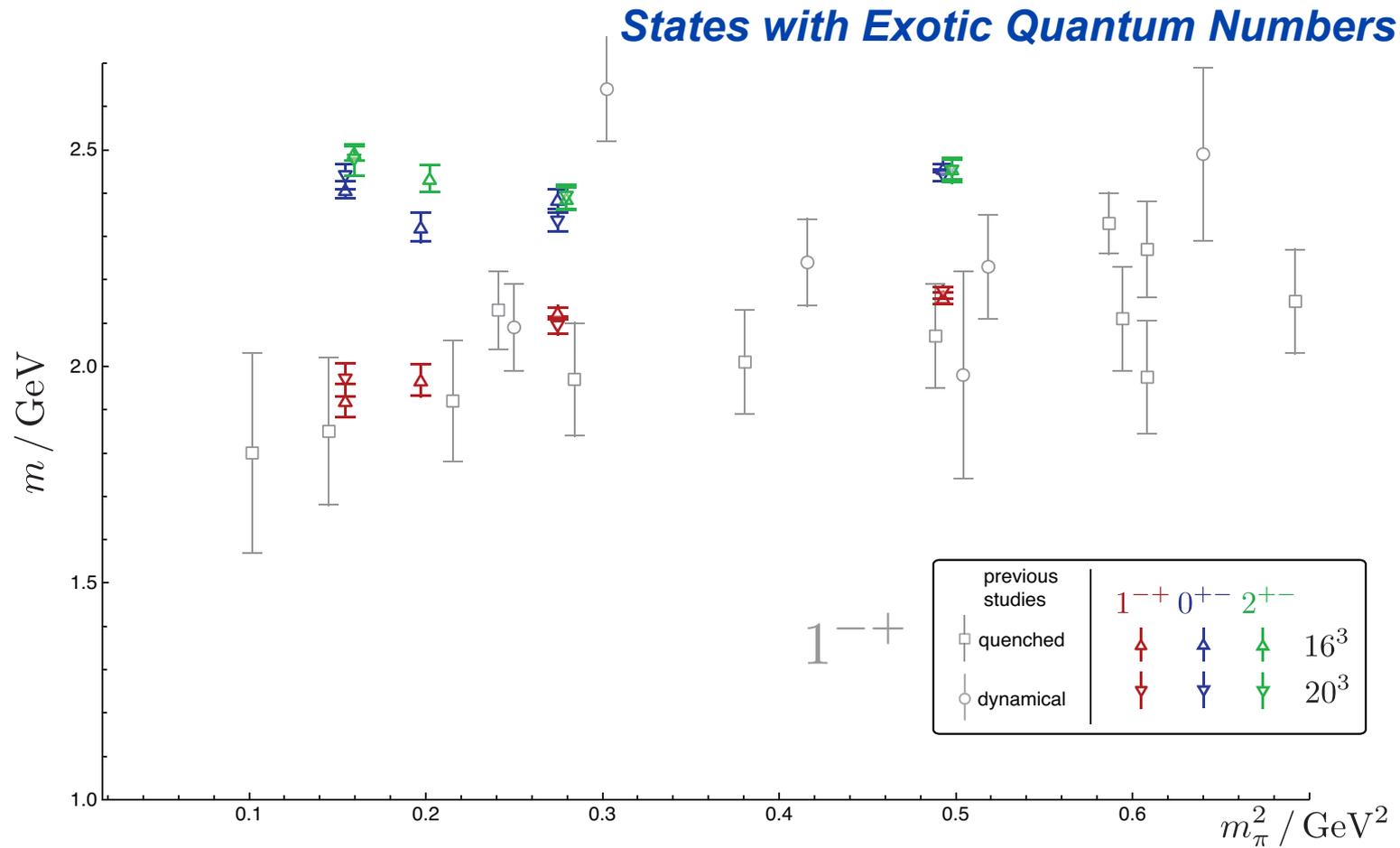
Isvector Meson Spectrum - I



PRL
103:262001,2009

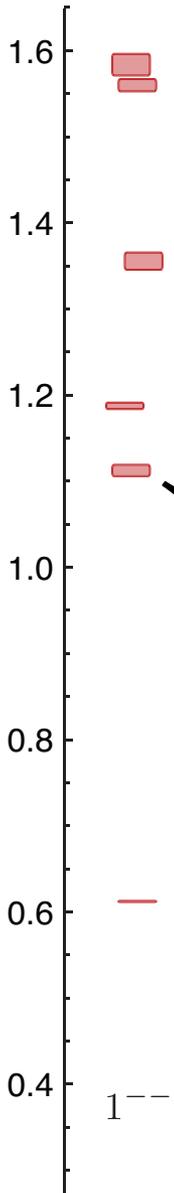
*Isvector spectrum
with quantum
numbers reliably
identified*

Isvector Meson Spectrum - II

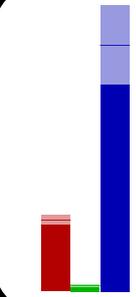


1⁻⁻⁻

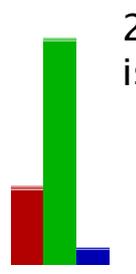
m/m_Ω



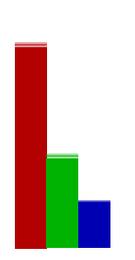
3rd excited state is dominantly hybrid?
with some 3S_1



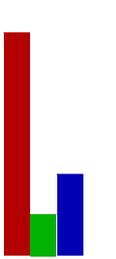
2nd excited state is dominantly 3D_1
with some 3S_1



1st excited state is dominantly 3S_1
with some 3D_1



ground state is dominantly 3S_1

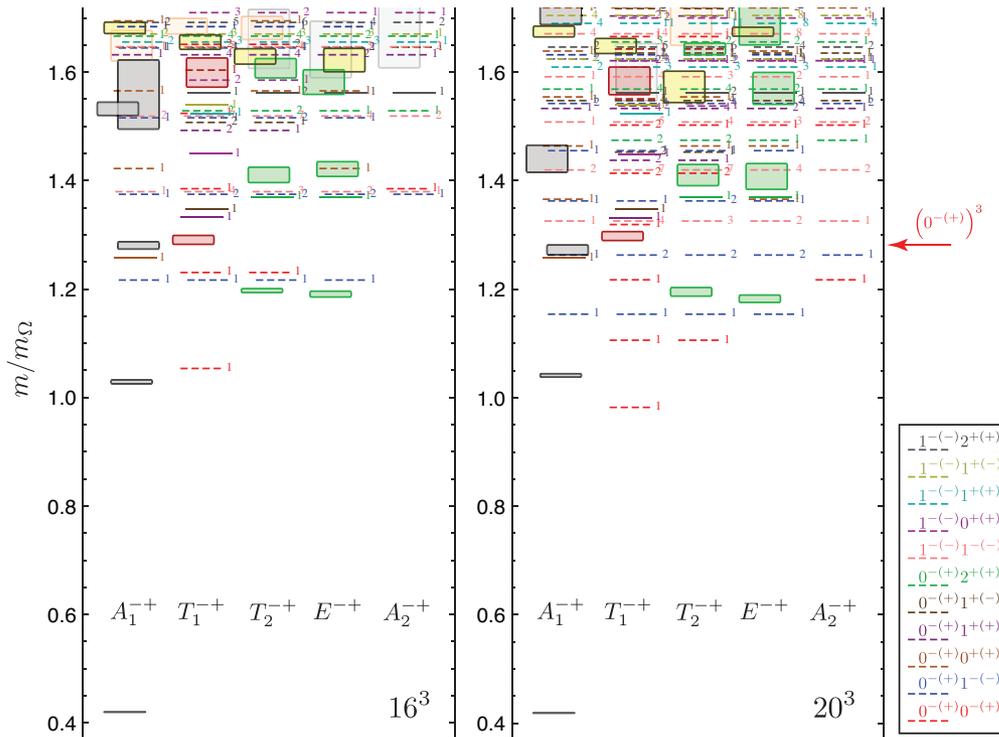


look at the 'overlaps' $Z_n^\Gamma = \langle n | \bar{\psi} \Gamma \psi | 0 \rangle$

ρ 3S_1
 $(\rho \times D_{J=2}^{[2]})^{J=1}$ 3D_1
 $(\pi \times D_{J=1}^{[2]})^{J=1}$ hybrid?

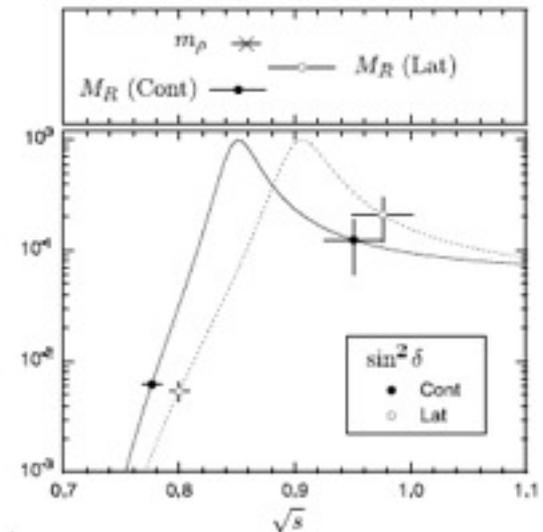
build a **bound state model**
phenomenology
comparable to the quark model
using non-perturbative **QCD**
calculations

Where are the multi-hadrons?



Meson spectrum on two volumes: dashed lines denote expected (non-interacting) multi-particle energies.

- Interacting particles: energies shifted by an amount that depends on E .
- Luscher: relates shift in the free-particle energy levels to phase shift at E .

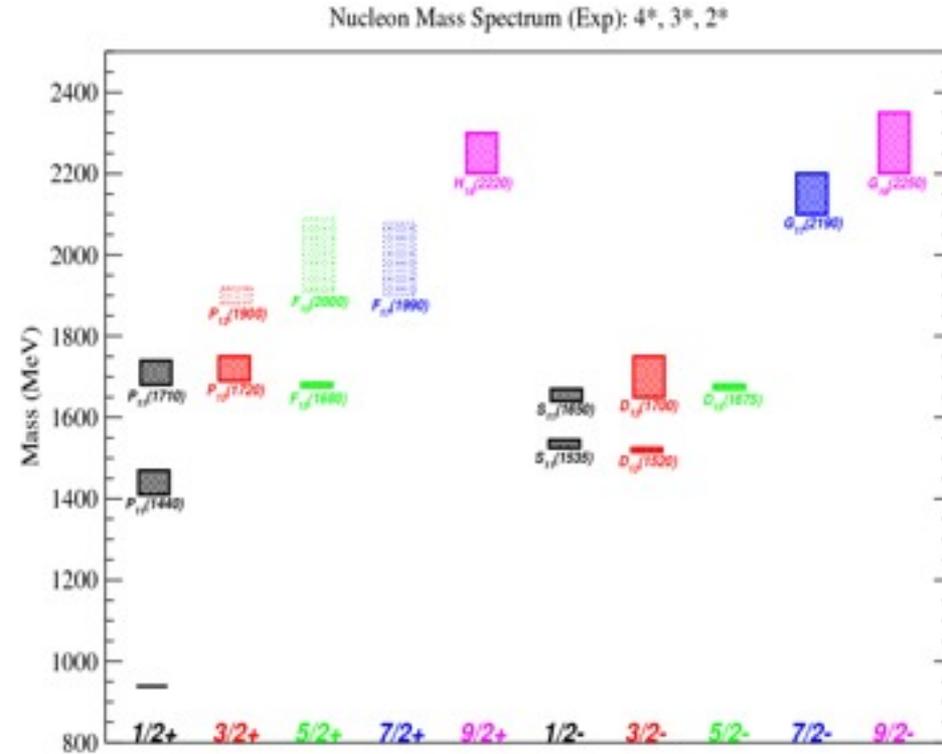
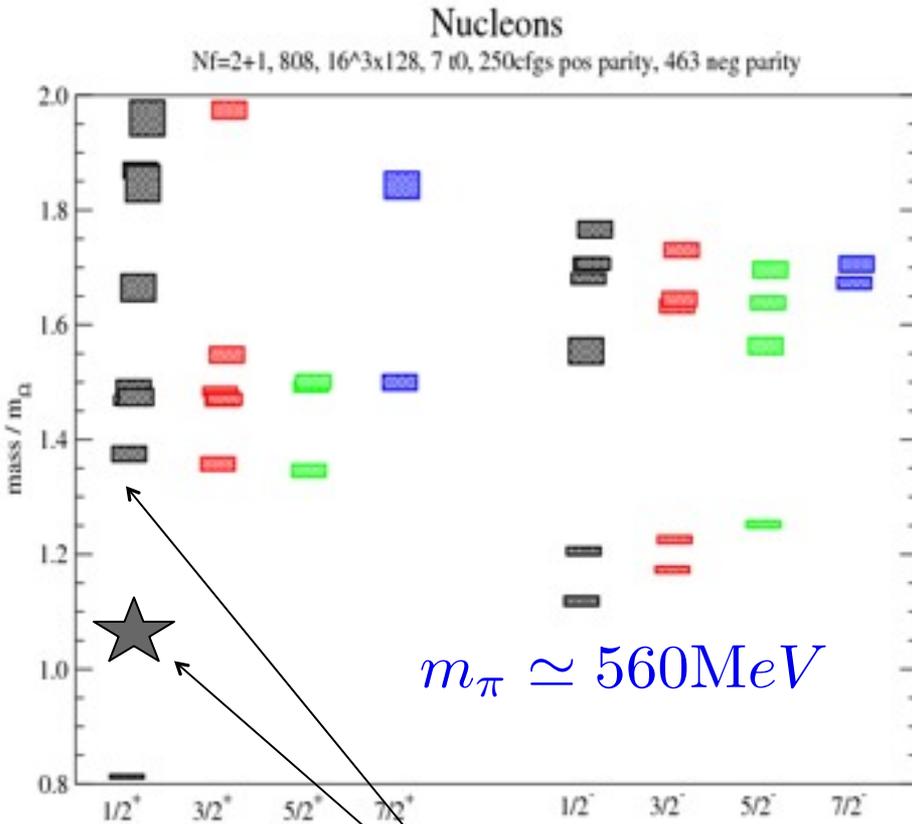


CP-PACS, arXiv:0708.3705

Calculation is incomplete.

Excited Baryon Spectrum

Subduction of continuum operators - reliable determination of baryon spins



Where is the "Roper"?

Thresholds & decays: need multi-particle ops

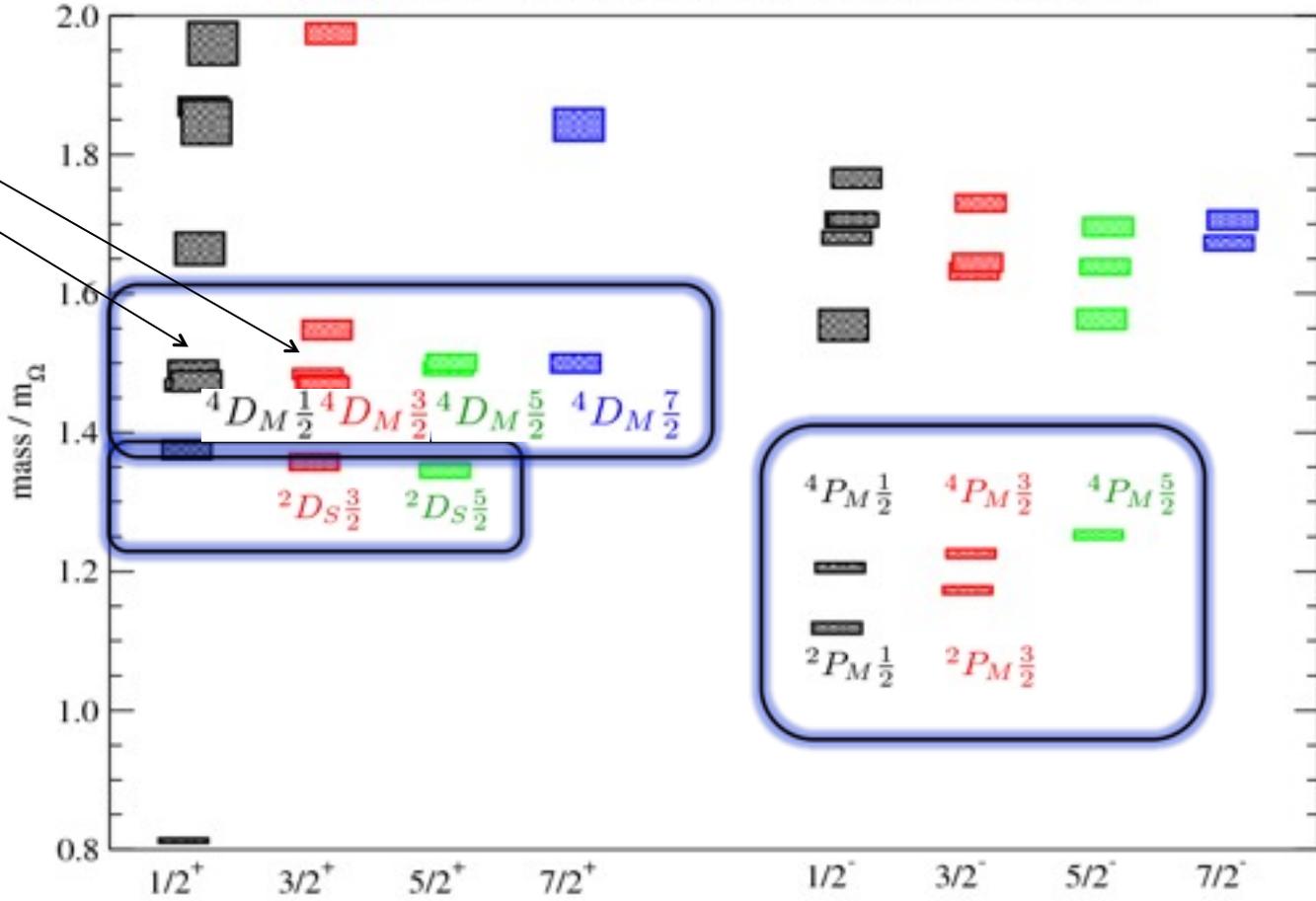
R. Edwards, Hadron 2009

Phenomenology: Nucleon Spectrum

Looks like quark model?

Compare overlaps & QM mixings

[20,1⁺]
P-wave
[70,2⁺]
D-wave
[56,2⁺]
D-wave



[70,1⁻]
P-wave

Summary

- Spectroscopy of Heavy Flavors affords an excellent theatre in which to study QCD, and in particular in a region where a non-relativistic picture may provide a faithful description.
- Lattice calculations can be used to construct a new “phenomenology” of QCD.
- Major challenge for lattice QCD:
 - Complete the calculation: where are the multi-hadrons?
 - Determine the phase shifts - model dependent extraction of resonance parameters

IF OUR UNDERSTANDING OF QCD IS CORRECT,
PRECISE LATTICE CALCULATIONS SHOULD CONFRONT
EXPERIMENT