

SPC Flavor Summary

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USQCD All Hands Meeting
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Introduction



- ◆ Caveat: This has not been reviewed by the SPC, so please don't blame the rest of the SPC for anything you do not like.
- ◆ Goals:
 - Brief summary of 2017 B physics proposals
 - Discussion of some of the physics opportunities to pin down the CKM matrix, test the Standard Model, search for evidence of new physics

Proposals

- ◆ Determination of $|V_{cb}|$ from Semi-leptonic Decays $B \rightarrow D^{(*)} l \nu$ using the Oktay-Kronfeld Action; PI: Gupta, 26 M J-Psi core-hr
- ◆ Investigation of $B \rightarrow K \pi l^+ l^-$ Decays with Lattice QCD; PI: Leskovec, 18.9 M J-Psi core-hr
- ◆ Standard Model Parameters and the Search for Physics Beyond the Standard Model with HISQ; PI: Mackenzie, 87.4 M J-Psi core-hr + 5.7 M BG/Q core-hr
- ◆ Semi-leptonic B and B_s -decays with charming hadronic final state; PI: Soni, 17.6 M J-Psi core-hr
- ◆ The following slides will summarize the goals of each proposal.

Gupta

- ◆ Uses Oktay-Kronfeld heavy quark action for b and c quarks
- ◆ MILC HISQ ensembles: three lattice spacings and three values of pion mass at each lattice spacing.
- ◆ $a=0.15, 0.12$ fm done on local clusters. Time is for 250 configurations of $a=0.09$ fm $m_l/m_s=0.1$ and physical mass ensembles.
 - 2016 allocation used for $m_l/m_s=0.2$ ensemble
- ◆ Use truncated solver method
- ◆ Aim for 1.0% (1.1%) error for $B \rightarrow D^* \ell \nu$ ($B \rightarrow D \ell \nu$) form factors. Currently, 1.4% (1.2)%.
- ◆ More about $|V_{cb}|$ later...

Leskovec

- ◆ Studying rare flavor changing neutral current decay $B \rightarrow K \pi l^+ l^-$ in region of $K^*(892)$
- ◆ Uses 2+1 flavor dynamical clover ensemble with $a=0.114$ fm and $m_\pi=317$ MeV
- ◆ LHCb found anomalous angular dependence at low q^2 .
- ◆ Sensitive probe of beyond standard model physics.
- ◆ Previously K^* treated as a stable particle
- ◆ Use one large volume ($32^3 \times 96$) and several moving frames
- ◆ Continuation: about 285 configurations will be analyzed this year. Would like to get to 800 with new allocation.

Mackenzie

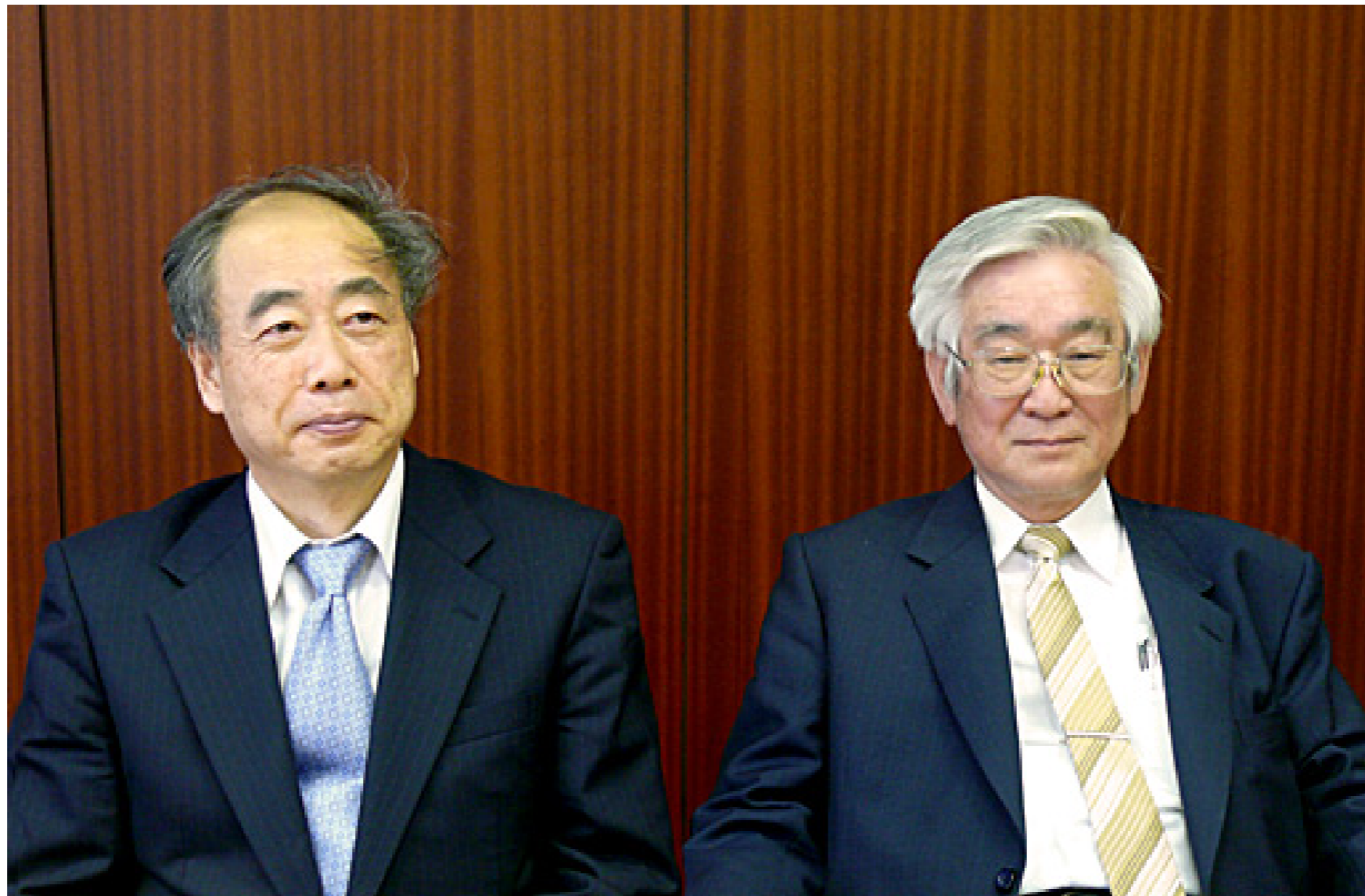
- ◆ Use 2+1+1 flavor HISQ ensembles; HISQ light valence quarks, Wilson/clover (w. FNAL interp.) b, c quarks; c quarks treated with HISQ as well for some projects
- ◆ Six lattice spacings: $a \approx 0.15, \mathbf{0.12}, \mathbf{0.09}, 0.06, 0.042, 0.03$ fm
- ◆ Physical light quark mass except for 0.03 fm ensemble
- ◆ Test CKM unitarity with broad range of decays:
 - ◆ $B \rightarrow \pi \ell \nu, B \rightarrow D^{(*)} \ell \nu, B_s \rightarrow D_s^{(*)} \ell \nu, K \rightarrow \pi \ell \nu, D \rightarrow \pi(K) \ell \nu$
 - ◆ neutral B meson mixing
 - ◆ $B \rightarrow \tau \nu, B \rightarrow D^{(*)} \tau \nu, B \rightarrow K^{(*)} \ell^+ \ell^-$
 - ◆ Decay constants for pseudoscalar and vector mesons
 - ◆ charm and bottom quark masses, α_s
- ◆ Aim for better precision than asqtad results

Soni

- ◆ Using Mobius domain-wall 2+1 flavor ensembles
- ◆ Seven ensembles with $0.114 \text{ fm} > a > 0.0711 \text{ fm}$, one with physical mass pion
- ◆ Relativistic heavy quark (RHQ) action
- ◆ $B \rightarrow D^{(*)} | \nu$, $B_s \rightarrow D_s^{(*)} | \nu$ to determine $|V_{cb}|$
- ◆ Light and strange quark propagators are already archived.
- ◆ Will run on two $48^3 \times 96$ ensembles with $a=0.11$ and 0.07 fm , with pion mass 138 and 234, respectively.
 - ◆ Three other ensembles already analyzed.
- ◆ Will later compute B meson mixing, & decay constants

Kobayashi & Maskawa

- ◆ Won 2008 Nobel prize for realization that with three (or more) generations can have CP violation, which might explain baryon asymmetry of Universe.



CKM Matrix

- ◆ Some relevant processes listed under each element

$$\left(\begin{array}{ccc}
 \mathbf{V}_{ud} & \mathbf{V}_{us} & \mathbf{V}_{ub} \\
 \pi \rightarrow l\nu & K \rightarrow \pi l\nu & B \rightarrow \pi l\nu \\
 & K \rightarrow l\nu & \\
 \mathbf{V}_{cd} & \mathbf{V}_{cs} & \mathbf{V}_{cb} \\
 D \rightarrow \pi l\nu & D \rightarrow K l\nu & B \rightarrow D^{(*)} l\nu \\
 D \rightarrow l\nu & D_s \rightarrow l\nu & \\
 \mathbf{V}_{td} & \mathbf{V}_{ts} & \mathbf{V}_{tb} \\
 \langle B_d | \bar{B}_d \rangle & \langle B_s | \bar{B}_s \rangle &
 \end{array} \right)$$

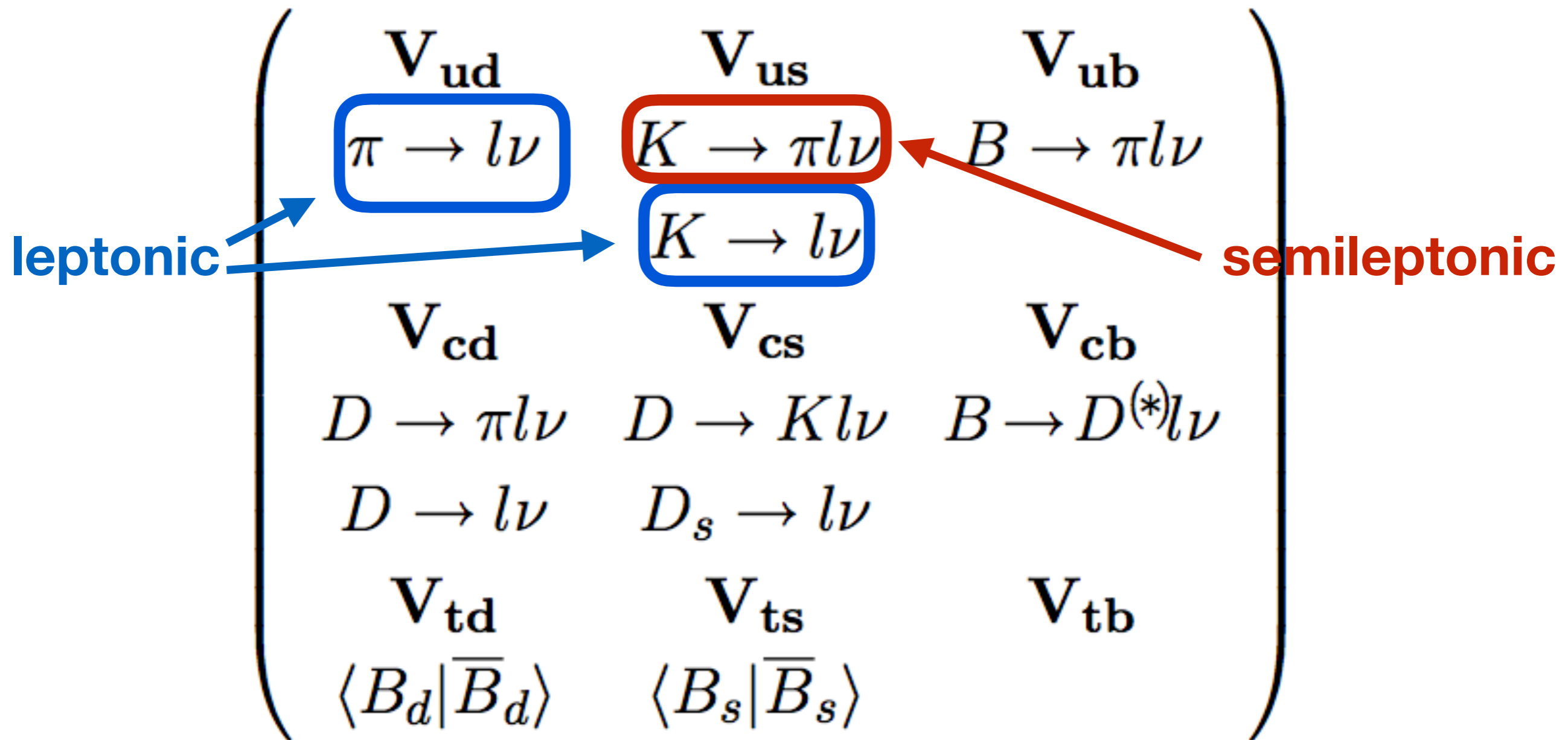
CKM Matrix II

- ◆ CKM matrix is unitary.
 - Each row and column is a (complex) unit vector.
 - Each row (column) is orthogonal to the other rows (columns).
- ◆ Violations of unitarity are evidence of non-standard model physics.
- ◆ If two different processes are used to determine an element of the matrix and they do not agree, that is evidence for new physics.
- ◆ LQCD input for decay constants and form factors is needed to determine elements of CKM matrix

$$\mathcal{B}(D_{(s)} \rightarrow \ell \nu_\ell) = \frac{G_F^2 |V_{cq}|^2 \tau_{D_{(s)}}}{8\pi} f_{D_{(s)}}^2 m_\ell^2 m_{D_{(s)}} \left(1 - \frac{m_\ell^2}{m_{D_{(s)}}^2} \right)^2$$

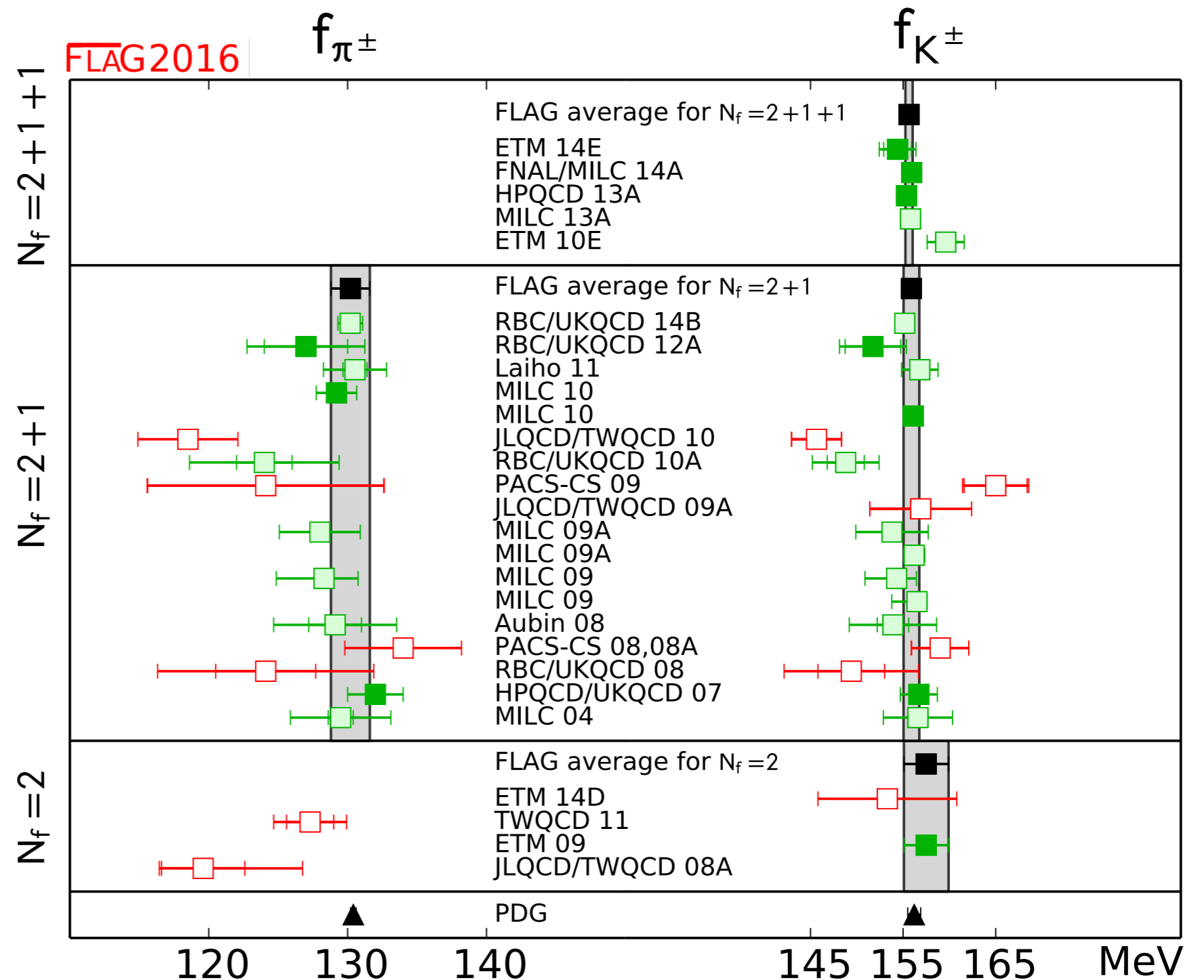
First Row: Light Quarks

- ◆ Processes involving only light quarks test first row unitarity



f_π and f_K

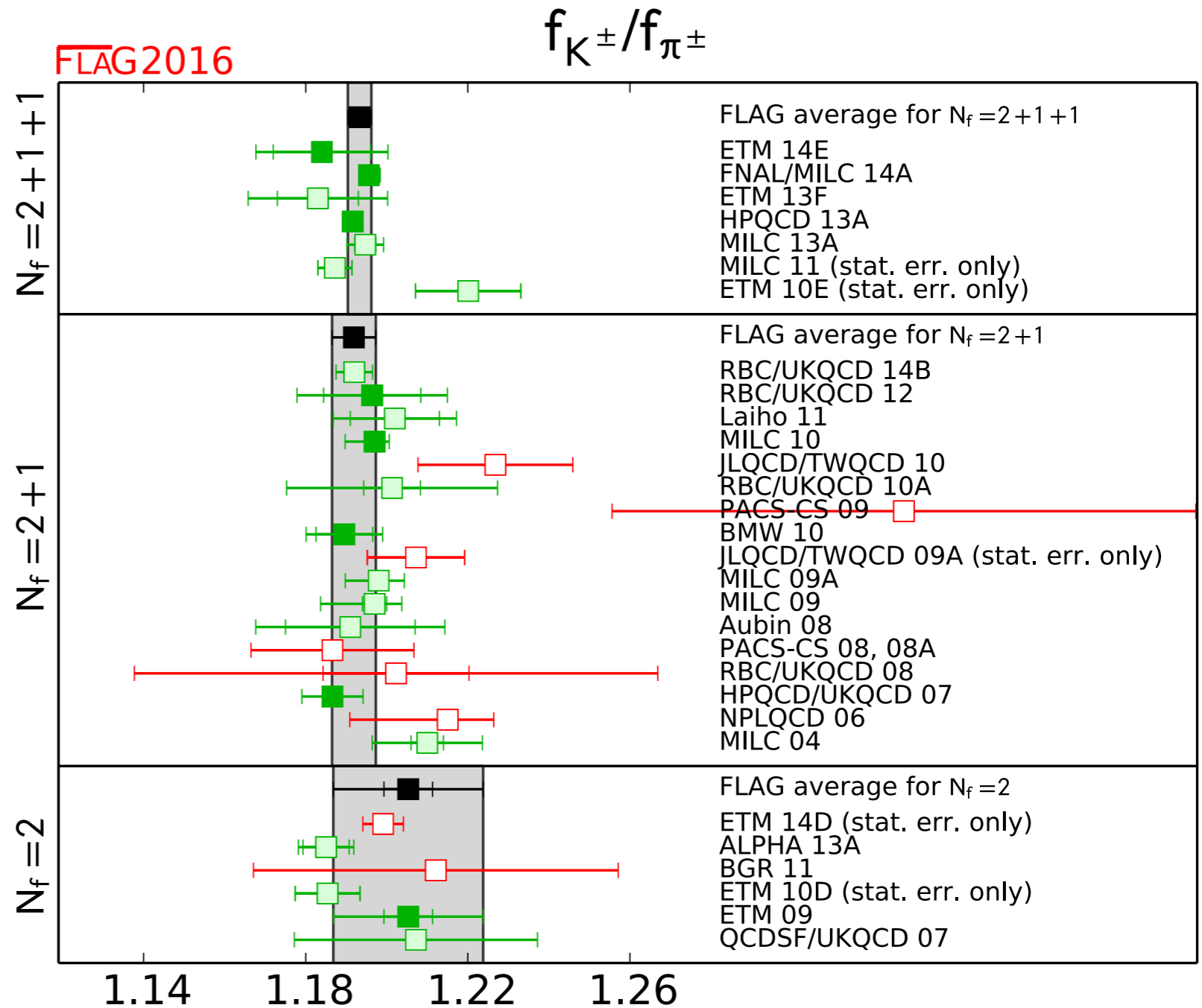
- Light decay constants as summarized by FLAG
- Some calcs. use f_π to set the scale so fewer results on left
- Ratio of decay constants is easy to calculate and used to test unitarity



f_{π}/f_K

- Light decay constant ratio summarized by FLAG
- From experimental measurement:

$$\left| \frac{V_{us}}{V_{ud}} \right| \frac{f_{K^{\pm}}}{f_{\pi^{\pm}}} = 0.2758(5)$$



K semileptonic decay

- ◆ Semileptonic decays have three-body final states, so there is one kinematic variable, usually denoted q^2 , which is momentum transfer to the leptons.

$$p_K = p_\pi + q_\ell + q_\nu$$

$$q = q_\ell + q_\nu$$

- ◆ To extract $|V_{us}|$ we just need $f_+(0)$ as experiment tells us

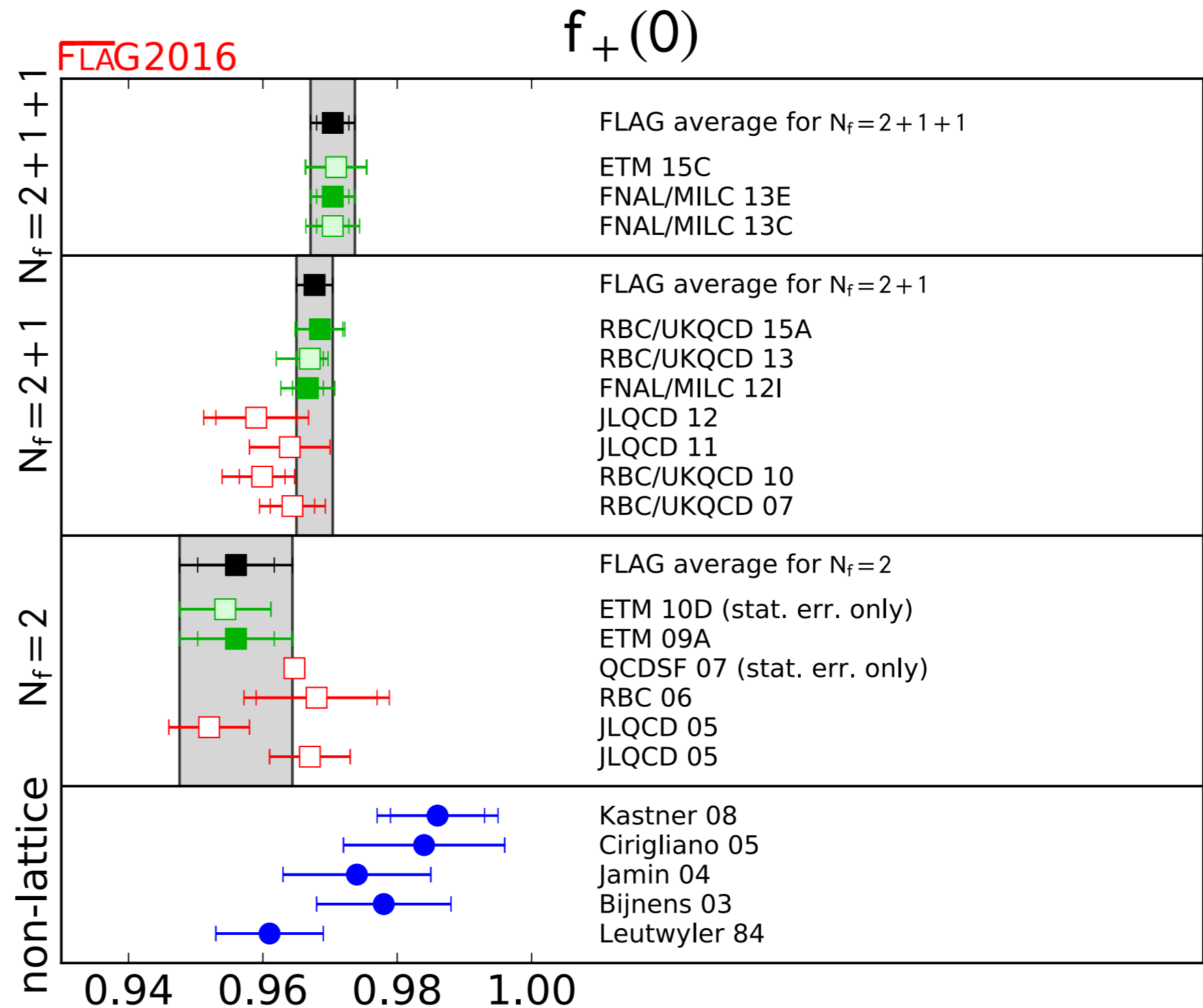
$$|V_{us}|f_+(0) = 0.2163(5)$$

- ◆ From FNAL/MILC with 2+1+1 flavors PRL 112, 112001 (2014),
arXiv:1312.1228 (0.34 % error)

$$f_+(0) = 0.9704(24)(22)$$

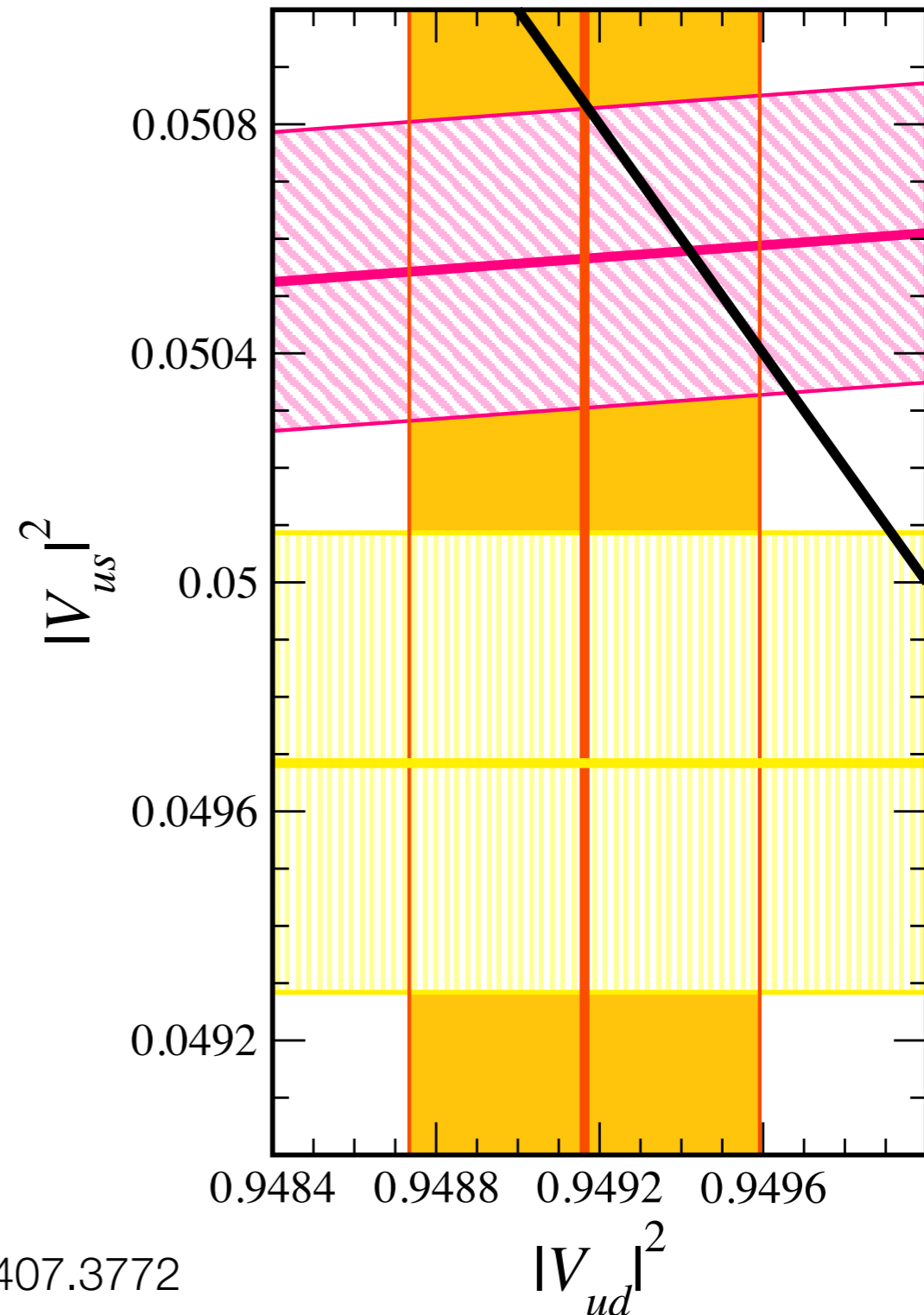
$f_+(0)$ for Kaon Decay

- FLAG averages for Kaon decay constant at $q^2=0$
- Only one value for $N_f=2, 2+1+1$
- Two values for $N_f=2$
- Next, we look at unitarity test



First Row Unitarity Test

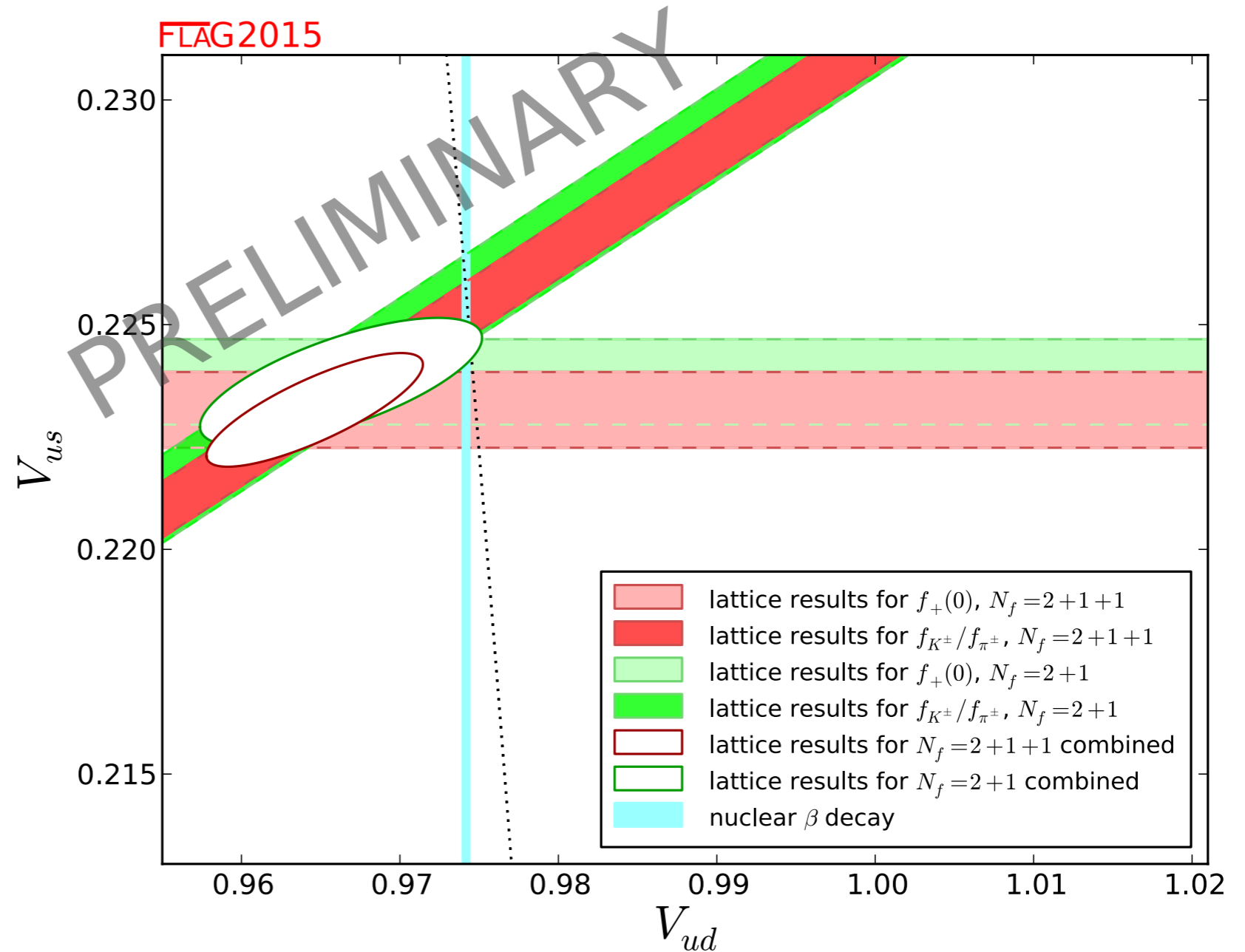
- Black line is unitarity
- Vertical band is from nuclear β decay (LQCD independent)
- Angled band is from leptonic decays
- Horizontal band is from semileptonic K decay
- Some tension between the two types of decay for $2+1+1$.
- Can we reduce semileptonic error?
1611.04188



FNAL/MILC, Phys.Rev. D90 (2014) 7, 074509 arXiv:1407.3772

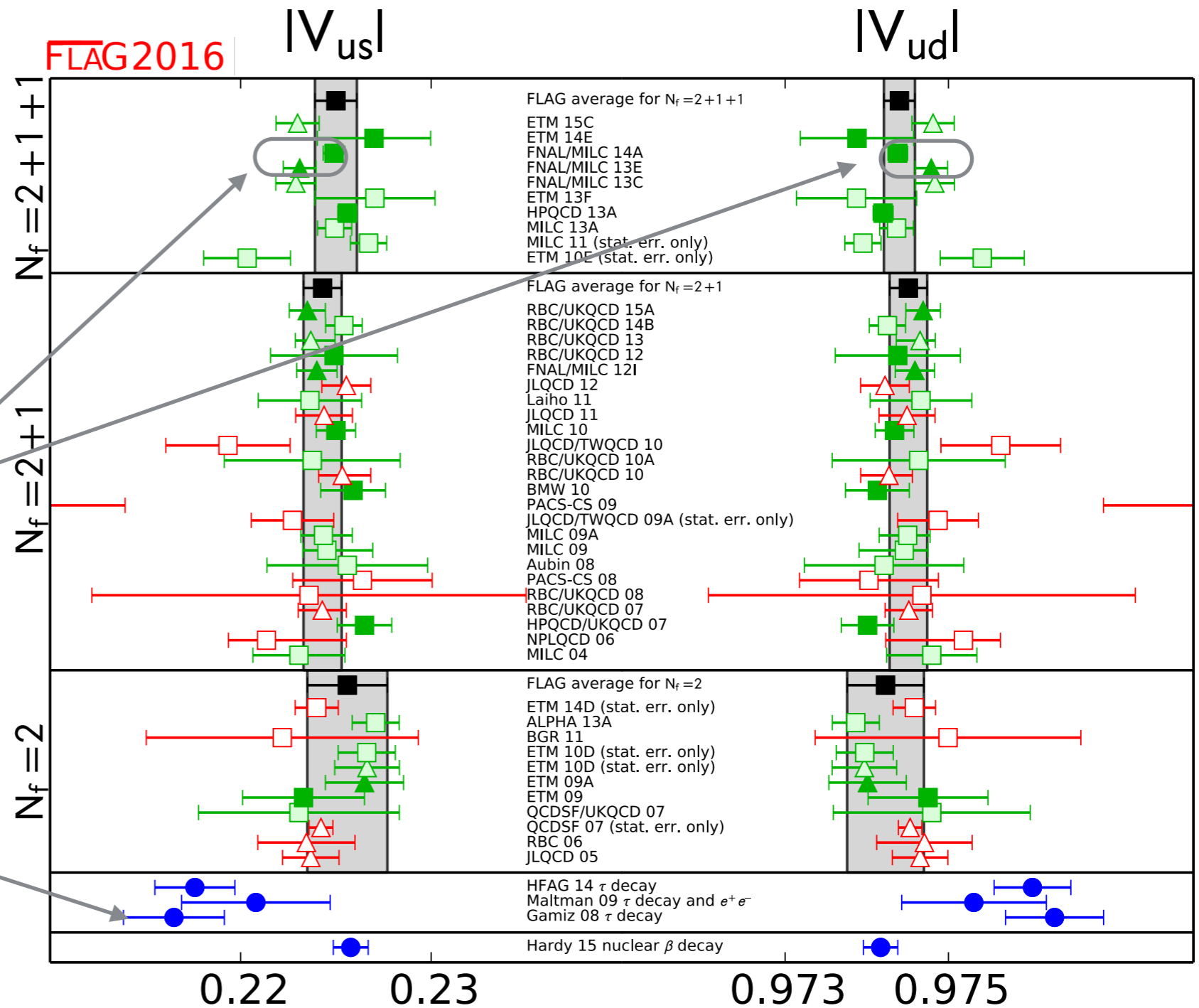
First Row Unitarity (FLAG)

- Preliminary FLAG3 results for 2+1 and 2+1+1 flavors
- Matrix elements not squared here
- Dotted line is unitarity
- 2+1 flavors has larger error and consistent with unitarity



$|V_{us}|$ & $|V_{ud}|$ Summary

- plot from FLAG
- squares leptonic
- triangles semileptonic
- good agreement w. 2+1 flavors, some tension for 2+1+1
- note tension between τ decay results and π and K decays



Second Row: Charm Quark

- ◆ Processes involving charm quark test second row unitarity

$$\left(\begin{array}{ccc}
 \mathbf{V}_{ud} & \mathbf{V}_{us} & \mathbf{V}_{ub} \\
 \pi \rightarrow l\nu & K \rightarrow \pi l\nu & B \rightarrow \pi l\nu \\
 & K \rightarrow l\nu & \\
 \mathbf{V}_{cd} & \mathbf{V}_{cs} & \mathbf{V}_{cb} \\
 \boxed{D \rightarrow \pi l\nu} & \boxed{D \rightarrow K l\nu} & \boxed{B \rightarrow D^{(*)} l\nu} \\
 \boxed{D \rightarrow l\nu} & \boxed{D_s \rightarrow l\nu} & \\
 \mathbf{V}_{td} & \mathbf{V}_{ts} & \mathbf{V}_{tb} \\
 \langle B_d | \bar{B}_d \rangle & \langle B_s | \bar{B}_s \rangle &
 \end{array} \right)$$

leptonic → $D \rightarrow l\nu$
semileptonic ← $B \rightarrow D^{(*)} l\nu$

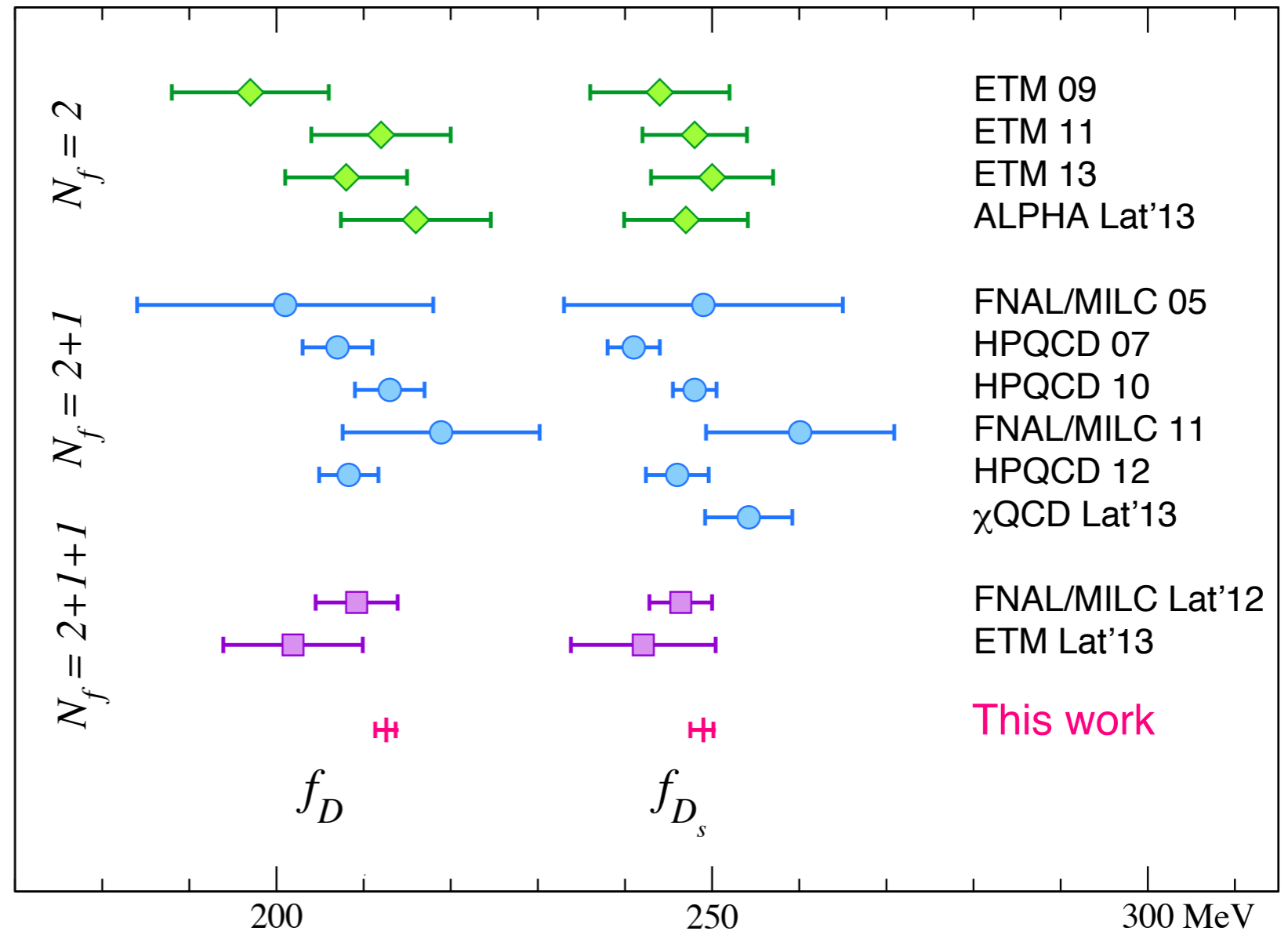
Charm Decay Constants

- Note improvement of precision from initial 2005 2+1 flavor results to current 2+1+1 flavor results.

$$f_{D^+} = 212.6(0.4) \begin{pmatrix} +1.0 \\ -1.2 \end{pmatrix} \text{ MeV}$$

$$f_{D_s} = 249.0(0.3) \begin{pmatrix} +1.1 \\ -1.5 \end{pmatrix} \text{ MeV}$$

- FLAG3 averages should be quite similar with slightly smaller errors

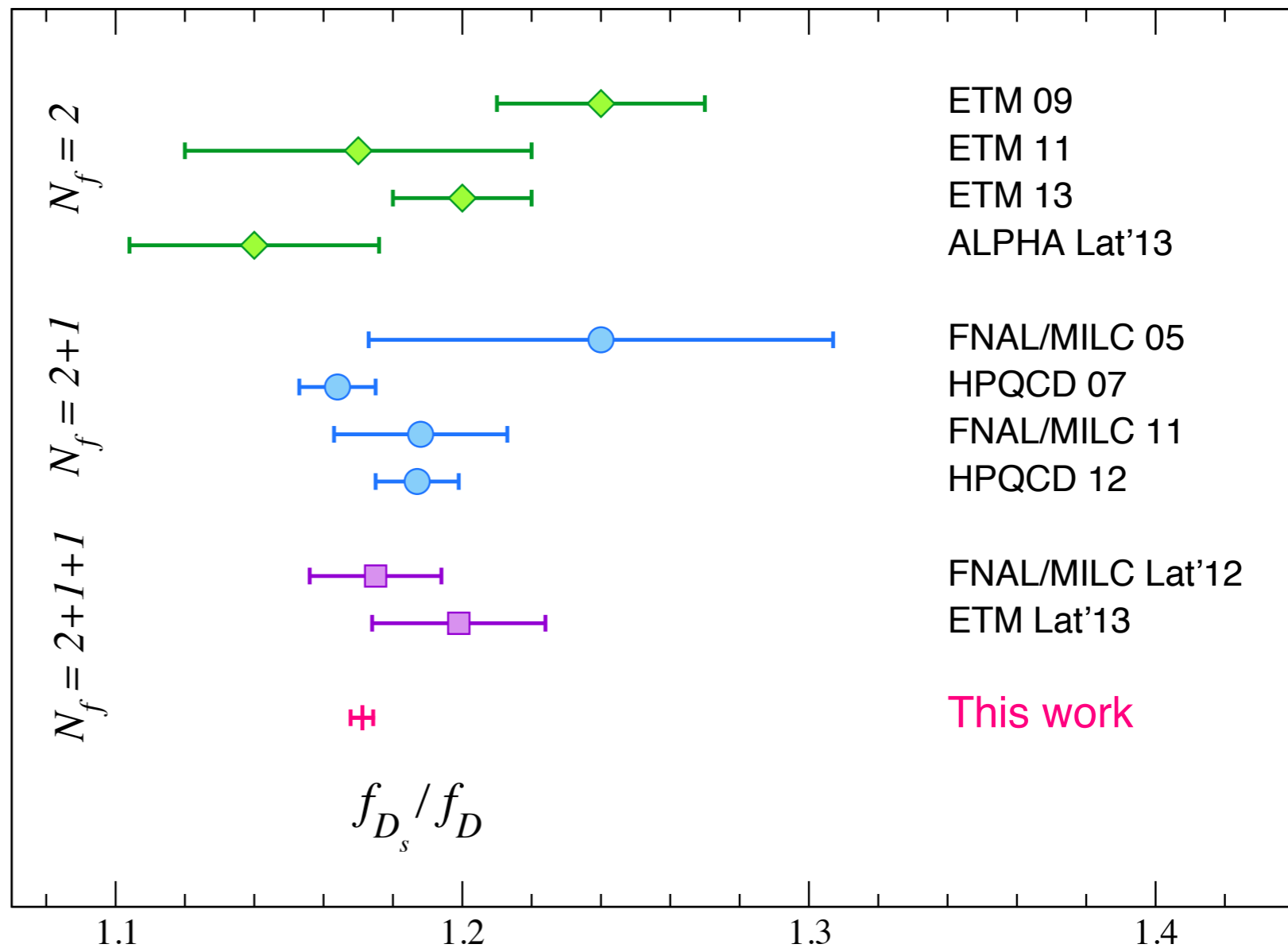


FNAL/MILC, Phys.Rev. D90 (2014) 7, 074509 arXiv:1407.3772

Charm Decay Constant Ratio

- Once again, note remarkable improvement over the past decade

$$f_{D_s} / f_{D^+} = 1.1712(10) \begin{pmatrix} +29 \\ -32 \end{pmatrix}$$



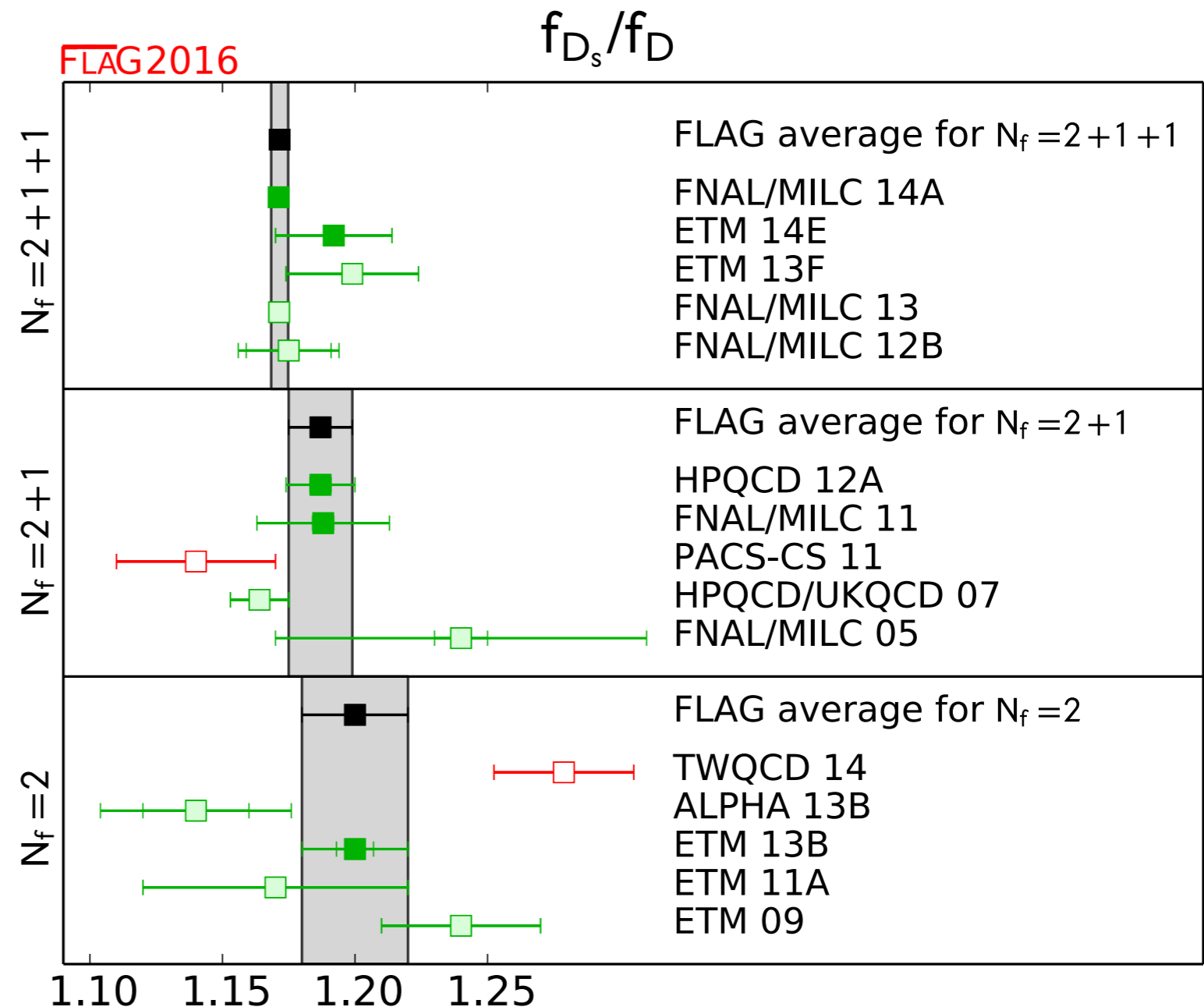
FNAL/MILC, Phys.Rev. D90 (2014) 7, 074509 arXiv:1407.3772

FLAG Charm Decay Constant Ratio

- Once again, note remarkable improvement over the past decade

$$f_{D_s}/f_{D^+} = 1.1712(10) \begin{pmatrix} +29 \\ -32 \end{pmatrix}$$

- FLAG 1.1716(32) for 2+1+1 flavors



Extraction of V_{cd} & V_{cs}

- ◆ The experimental results for charm meson leptonic decays are summarized by the Heavy Flavor Averaging Group (HFAG):

$$f_D |V_{cd}| = 46.40(1.98)\text{MeV}, \quad f_{D_s} |V_{cs}| = 253.1(5.3)\text{MeV}$$

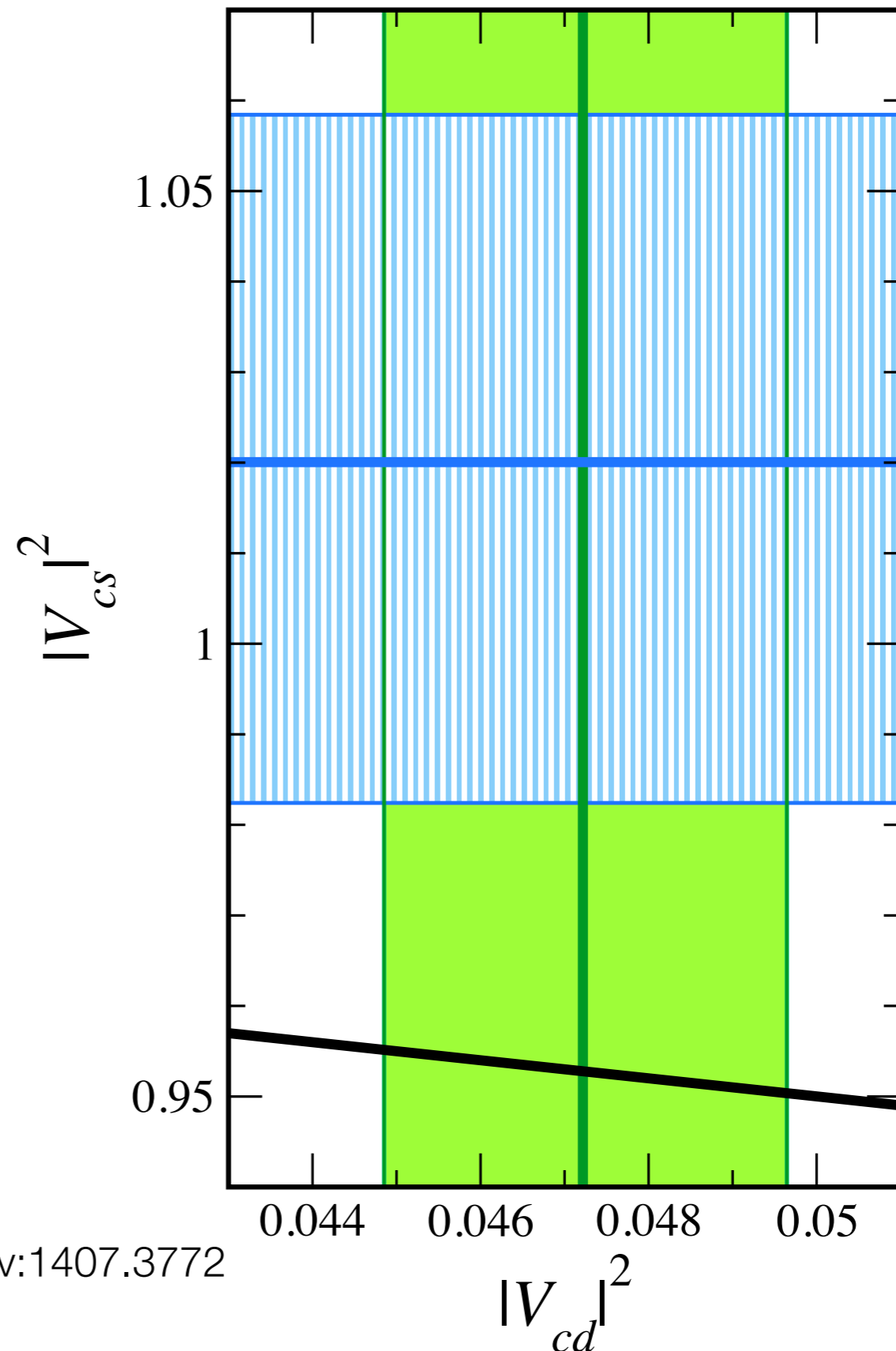
- ◆ Experimental error is 2.1-4.3%.
- ◆ Using decay constants from LQCD, we get CKM matrix elements:

$$|V_{cd}| = 0.217(1)(5)(1), \quad |V_{cs}| = 1.010(5)(18)(6)$$

- ◆ Errors are lattice, experiment, and structure dependent electromagnetic, respectively.

Second Row Unitarity

- Black line is unitarity
- Horizontal blue band is D_s leptonic decay
- Vertical green band is D^+ leptonic decay
- Note the $\approx 1.8 \sigma$ tension with unitarity
- Fajfer et al., PRD91, (2015) 094009 bound new physics
- Fewer results for semileptonic D meson decays
- Expt. error dominant now.



FNAL/MILC, Phys.Rev. D90 (2014) 7, 074509 arXiv:1407.3772

D semileptonic result

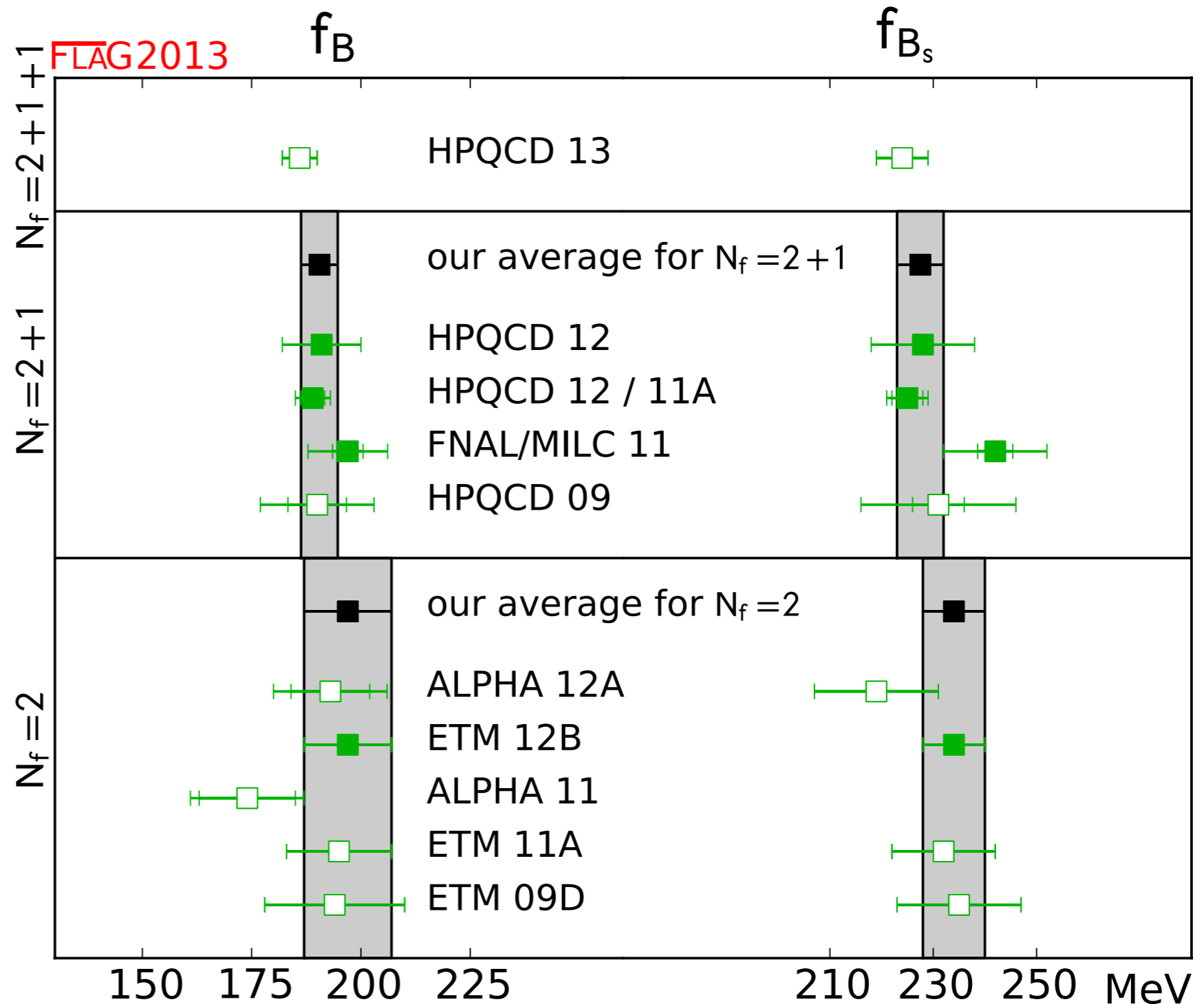
- ◆ Interestingly, there is a new BaBar paper, PRD91, 052022(2015), on semileptonic D decay that uses HPQCD result.
- ◆ It yields $|V_{cd}| = 0.206 \pm 0.007_{\text{exp}} \pm 0.009_{\text{LQCD}}$.
- ◆ Adding errors in quadrature $0.206(11)$ compared with our leptonic decay result of $0.217(5)$.
- ◆ Their central value is two of our sigma below our result, but our result is only one of their sigmas high.

B Meson Decays

- ◆ Leptonic and semileptonic decays studied in LQCD
- ◆ Rare decays involving flavor changing neutral currents (FCNC) also studied
 - FCNC vanish at tree level in Standard Model, so a good place to look for new physics
 - Some tension between recent SM prediction from LQCD and LHCb measurements
 - Alternative to B meson mixing for determining $|V_{td}|$ and $|V_{ts}|$

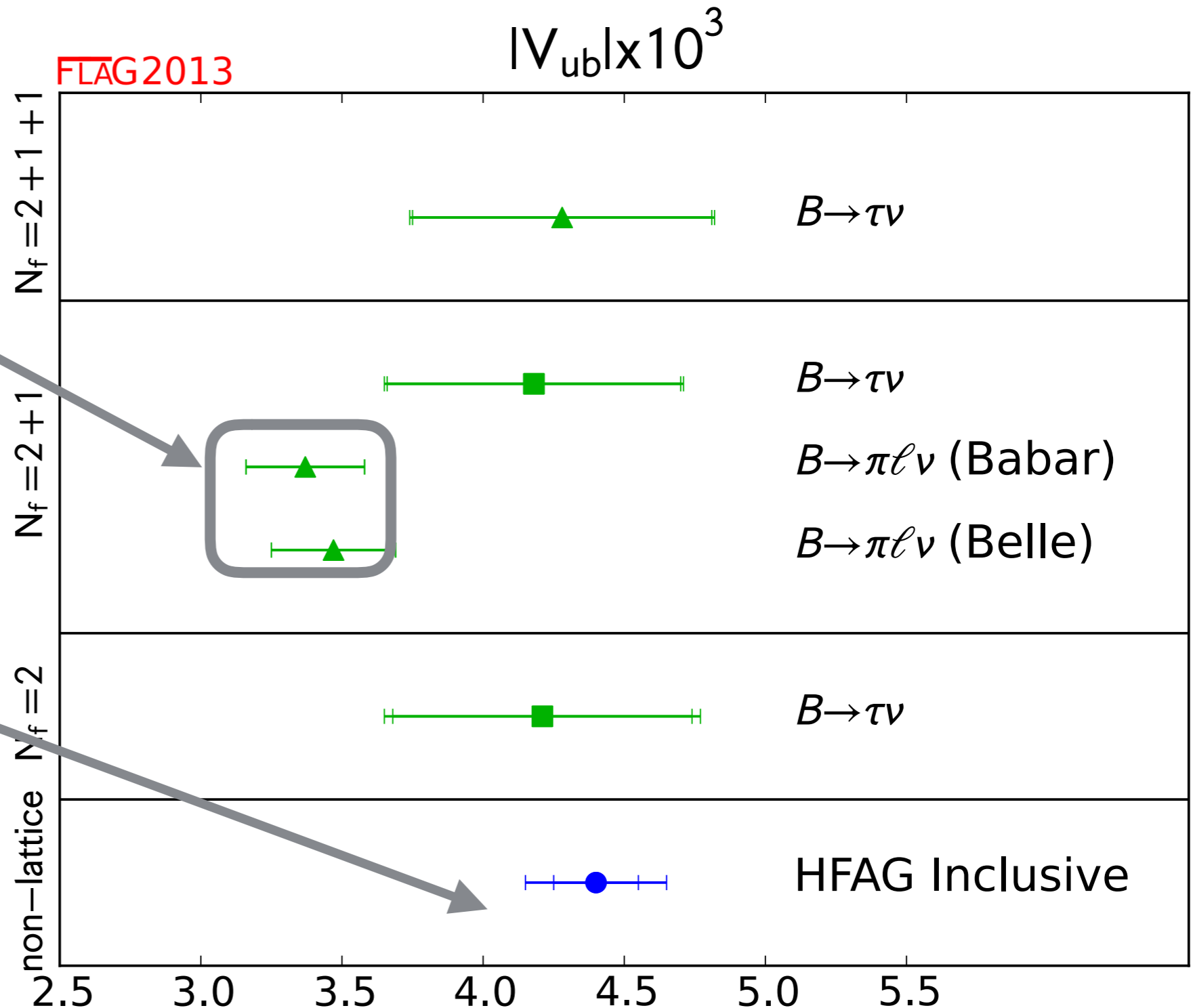
B Meson Leptonic Decays

- FLAG3 will have only minor updates to these results
 - RBC/UKQCD 2+1
 - ETM 2+1+1 (plotted)
 - both have large errors
- For 2+1 and 2+1+1 flavors errors about 2%
- $f_B = 190.5(4.2)$ MeV, $f_{B_s} = 227.7(4.5)$ MeV for 2+1 flavors (2013)



$|V_{ub}|$ from FLAG2

- Large errors for leptonic decays from experiment (25%)
- Semileptonic decays give smaller value
- Tension between exclusive and inclusive results
- Plot from T. Vladikas arXiv:1509.01155
- Belle II will improve $B \rightarrow \tau \nu$ measurement (5% error expected)



Exclusive B Decay Update

◆ FNAL/MILC updated form factors for semileptonic decays PRD 92, 014024 (2015), arXiv:1503.07839

◆ FLAG:

$$|V_{ub}| = 3.37(21) \times 10^{-3}, \quad N_f = 2 + 1; \text{BaBar}$$

$$|V_{ub}| = 3.47(22) \times 10^{-3}, \quad N_f = 2 + 1; \text{Belle}$$

◆ New FNAL/MILC result

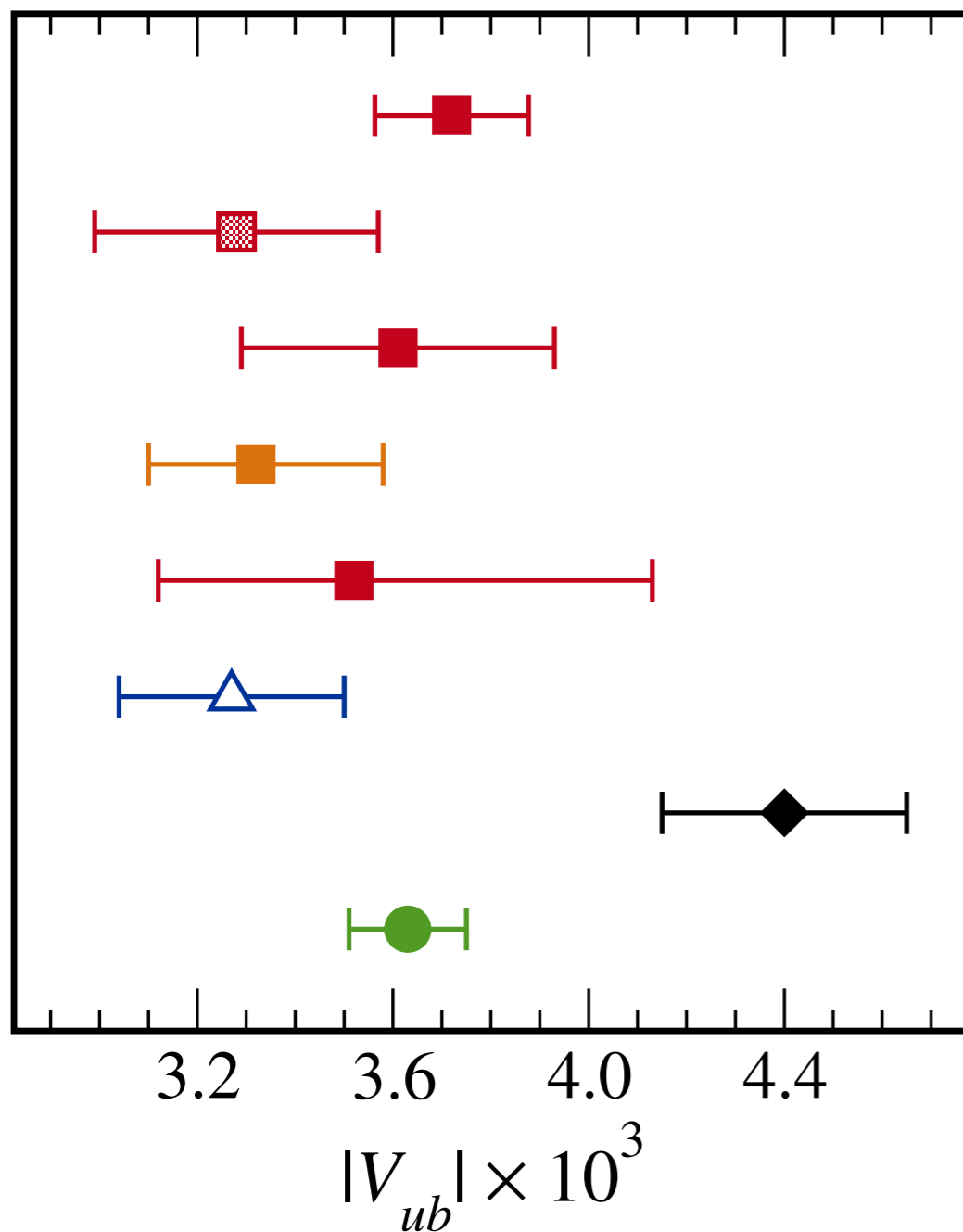
$$|V_{ub}| = 3.72(16) \times 10^{-3}, \quad N_f = 2 + 1; \text{BaBar\&Belle}$$

◆ This result decreases, but does not eliminate tension between exclusive and inclusive results.

◆ Next slide also includes Lambda baryon decay result

Updated Semileptonic $|V_{ub}|$

Lattice error now comparable to experimental error.



This work + BaBar + Belle, $B \rightarrow \pi l\nu$

Fermilab/MILC 2008 + HFAG 2014, $B \rightarrow \pi l\nu$

RBC/UKQCD 2015 + BaBar + Belle, $B \rightarrow \pi l\nu$

Imsong *et al.* 2014 + BaBar12 + Belle13, $B \rightarrow \pi l\nu$

HPQCD 2006 + HFAG 2014, $B \rightarrow \pi l\nu$

Detmold *et al.* 2015 + LHCb 2015, $\Lambda_b \rightarrow p l\nu$

BLNP 2004 + HFAG 2014, $B \rightarrow X_u l\nu$

UTFit 2014, CKM unitarity

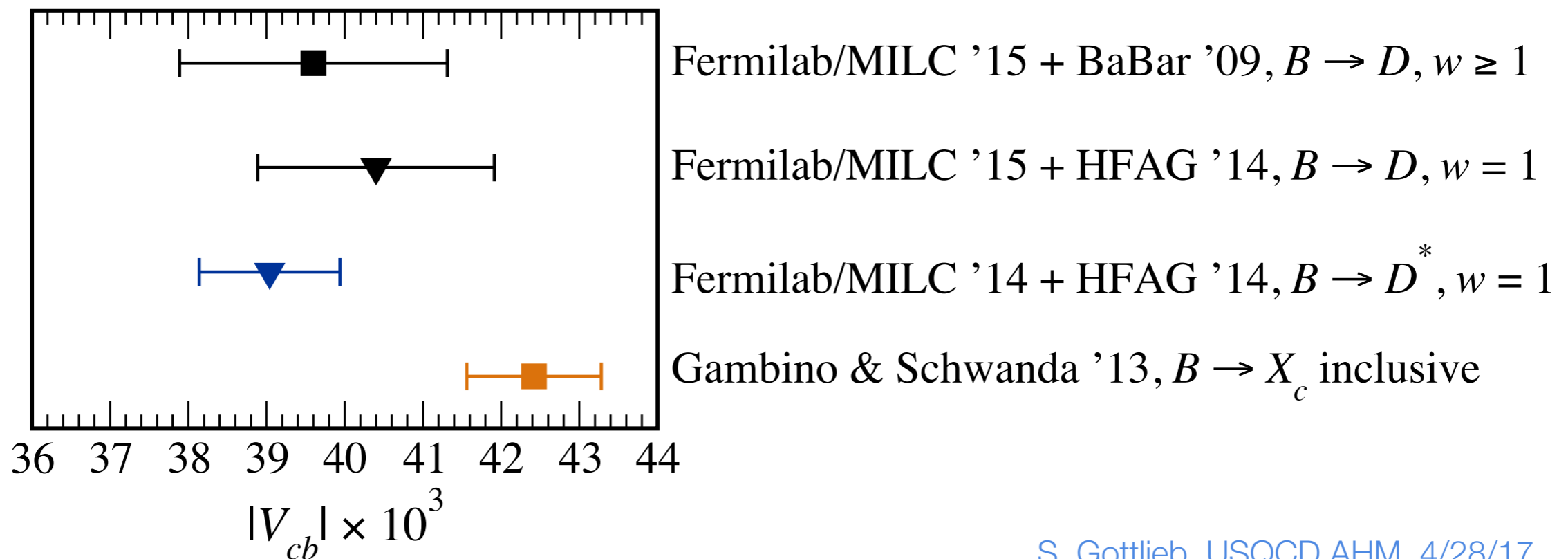
PRD 92, 014024 (2015), arXiv:1503.07839

$|V_{cb}|$

- ◆ Exclusive calculations of $B \rightarrow D^* | \nu$ and $B \rightarrow D | \nu$ yield V_{cb}
- ◆ Experimental error dominant for $B \rightarrow D | \nu$ (3.9% vs 1.4%)
- ◆ Again, tension between exclusive and inclusive results

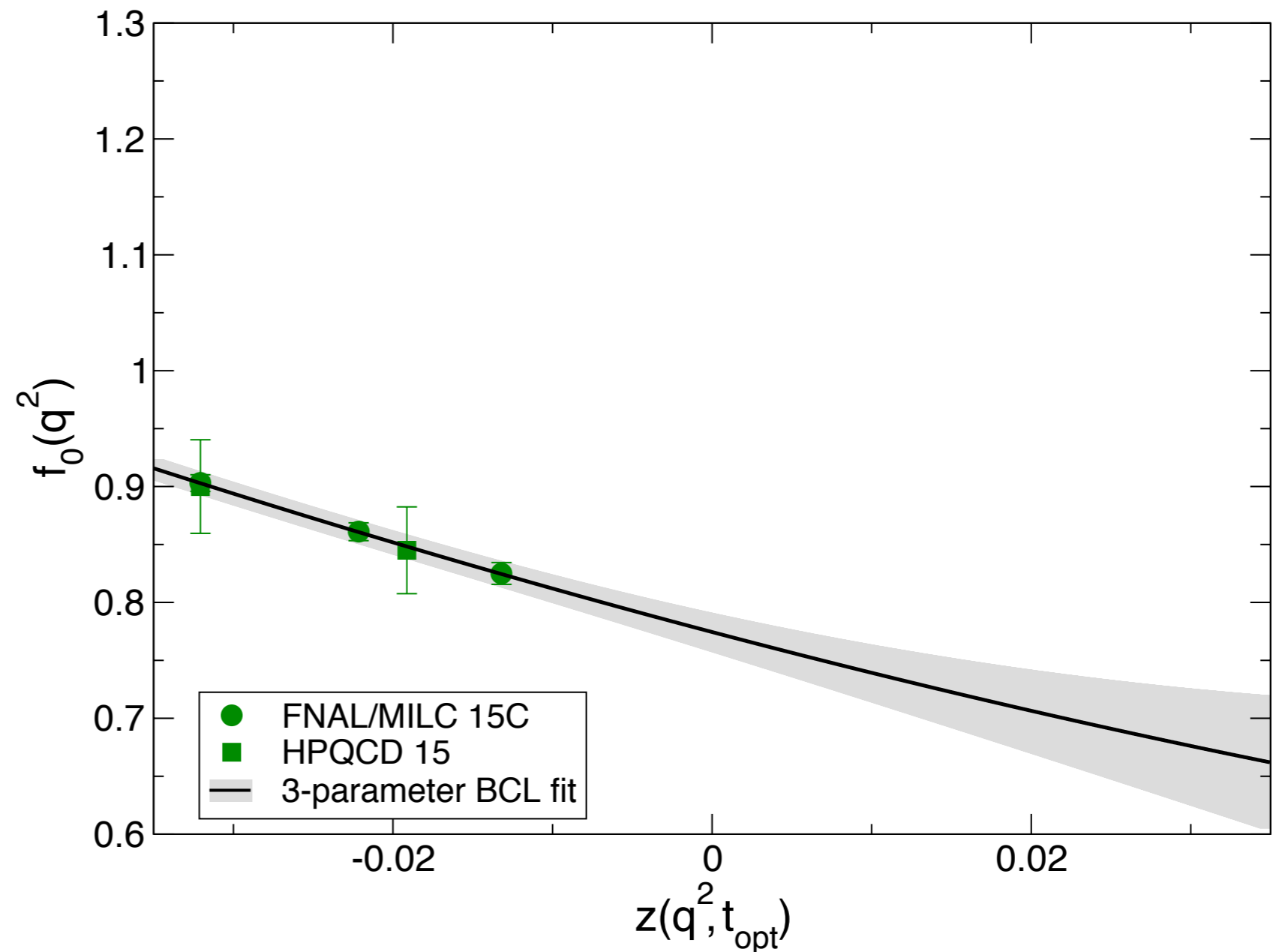
PRD 92, 034506 (2015), arXiv:1503.07237 [hep-lat]

- ◆ But two exclusive decay modes consistent



$B \rightarrow D \ell \nu$ form factor

- Two results with 2+1 flavors both on MILC asqtad ensembles.



V_{ub} and V_{cb} : exclusive vs inclusive

uses CLN parametrization

[Caprini, Lellouch, Neubert 9712417]

- Exclusive:

$$|V_{ub}|_{B \rightarrow \pi \ell \nu} = 3.73(14) \times 10^{-3} \quad \text{[FLAG]}$$

$$|V_{ub}|_{B \rightarrow \tau \nu} = 4.33(72) \times 10^{-3} \quad \text{[PDG+FLAG]}$$

$$|V_{cb}|_{B \rightarrow D \ell \nu} = 40.1(1.0) \times 10^{-3} \quad \text{[FLAG]}$$

$$\leftarrow |V_{cb}|_{B \rightarrow D^* \ell \nu} = 39.27(56)(49) \times 10^{-3} \quad \text{[FLAG]}$$

$$|V_{ub}/V_{cb}|_{\Lambda_b \rightarrow (p, \Lambda_c) \ell \nu} = 0.083(6) \quad \text{[PDG]}$$

[Detmold, Lehner, Meinel]

- Inclusive [PDG]:

$$|V_{ub}|_{B \rightarrow X_u \ell \nu} = 4.49(16) \left(\begin{smallmatrix} +16 \\ -18 \end{smallmatrix} \right) \times 10^{-3}$$

$$|V_{cb}|_{B \rightarrow X_c \ell \nu} = 42.2(0.7) \times 10^{-3}$$

- The overall tension between all these determinations is 3.2σ

- Future progress

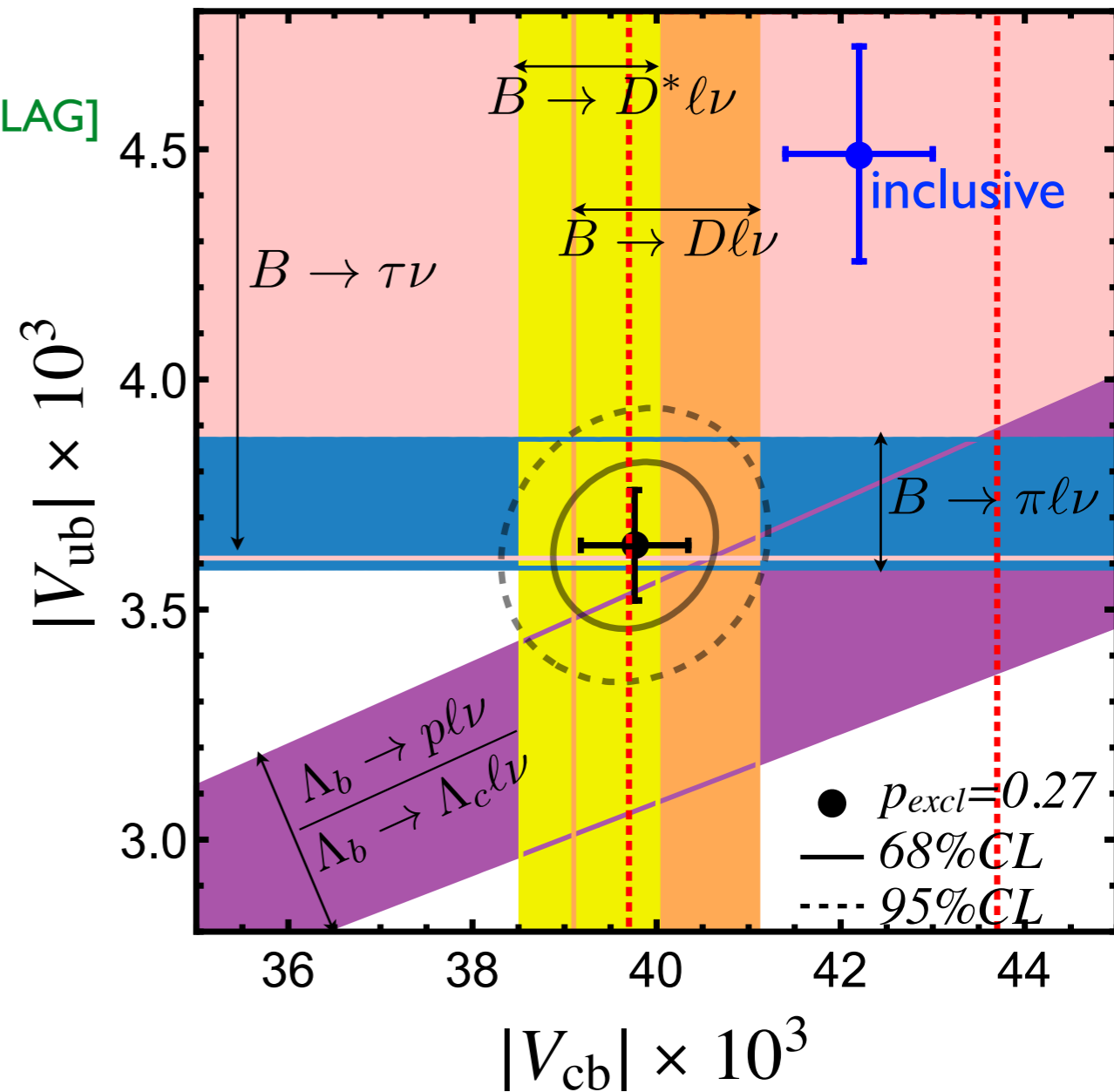
- ◆ $B \rightarrow D^*$ form factor: q^2 dependence and use

- of BCL/BGL parametrization [Berlochner et al. 1703.05330]

- [Bigi, Gambino, Schacht 1703.06124]

- ◆ $B_s \rightarrow K \ell \nu$

- [Grinstein, Kobach 1703.08170]



● $p_{excl}=0.27$

— 68%CL

- - - 95%CL

←→

$B \rightarrow D^* \ell \nu$

using the new Belle

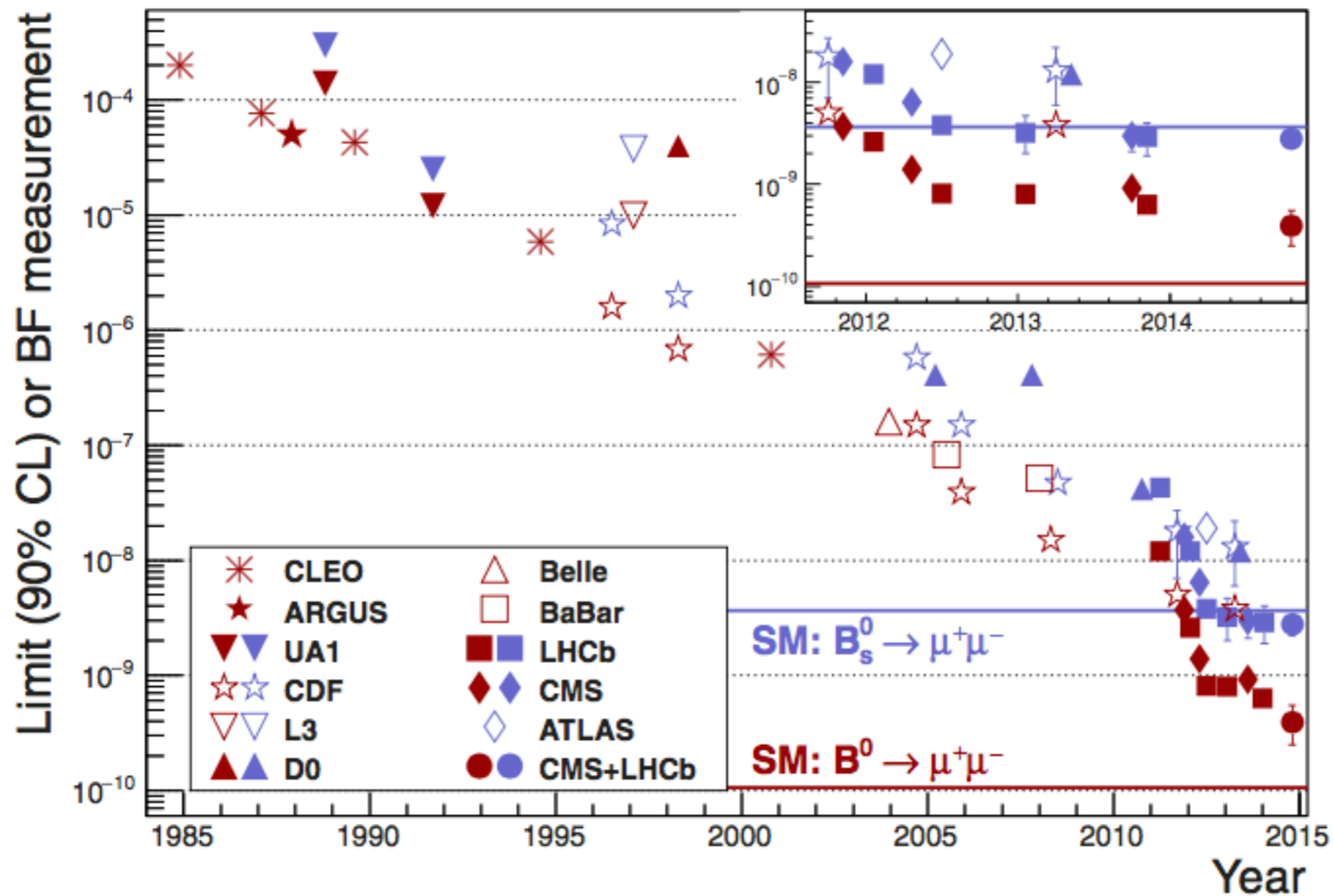
result 1702.01521

Ken Lane's List from LHCb

- ◆ $B^+ \rightarrow K^+ \mu^+ \mu^- / B^+ \rightarrow K^+ e^+ e^-$ $25\% < \text{SM}$ (2.6σ)
- ◆ Independently, $B^+ \rightarrow K^+ \mu^+ \mu^-$ branching ratio $30\% < \text{SM}$ (2σ)
- ◆ Earlier results for electron mode consistent with SM
 - Lepton nonuniversality may not demand much more from LQCD, i.e., BSM physics will change Wilson coefficients. (pheno ms.)
- ◆ $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular distribution differs from SM by 2.9σ in two bins. Theoretical error questioned.
 - We have not done this decay. (Not gold plated...)
- ◆ $B_{(s)} \rightarrow \mu^+ \mu^-$ branching ratios jointly measured by CMS and LHCb ...

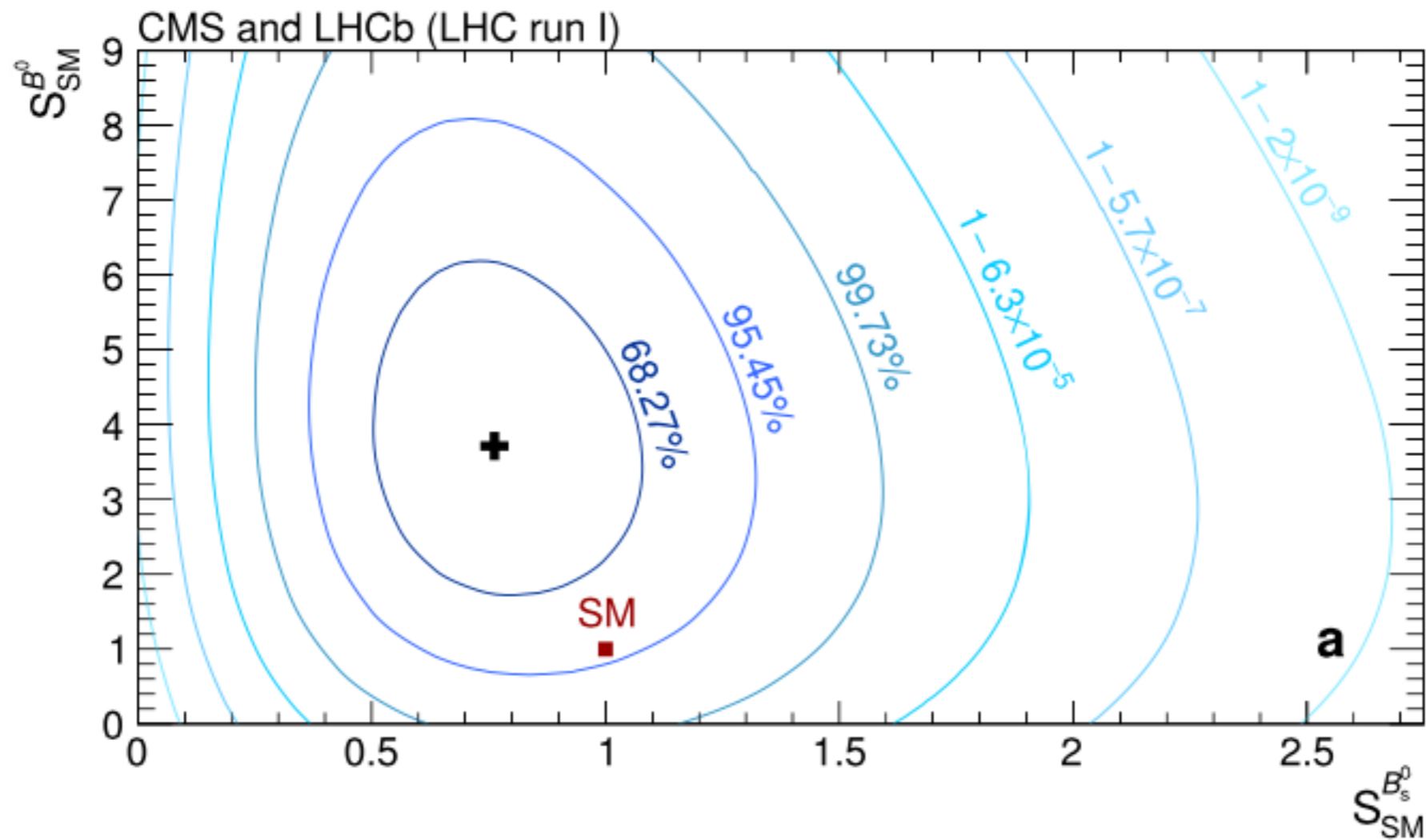
$$B_{(s)} \rightarrow \mu^+ \mu^-$$

◆ Nature: doi:10.1038/nature14474 (we're cited)



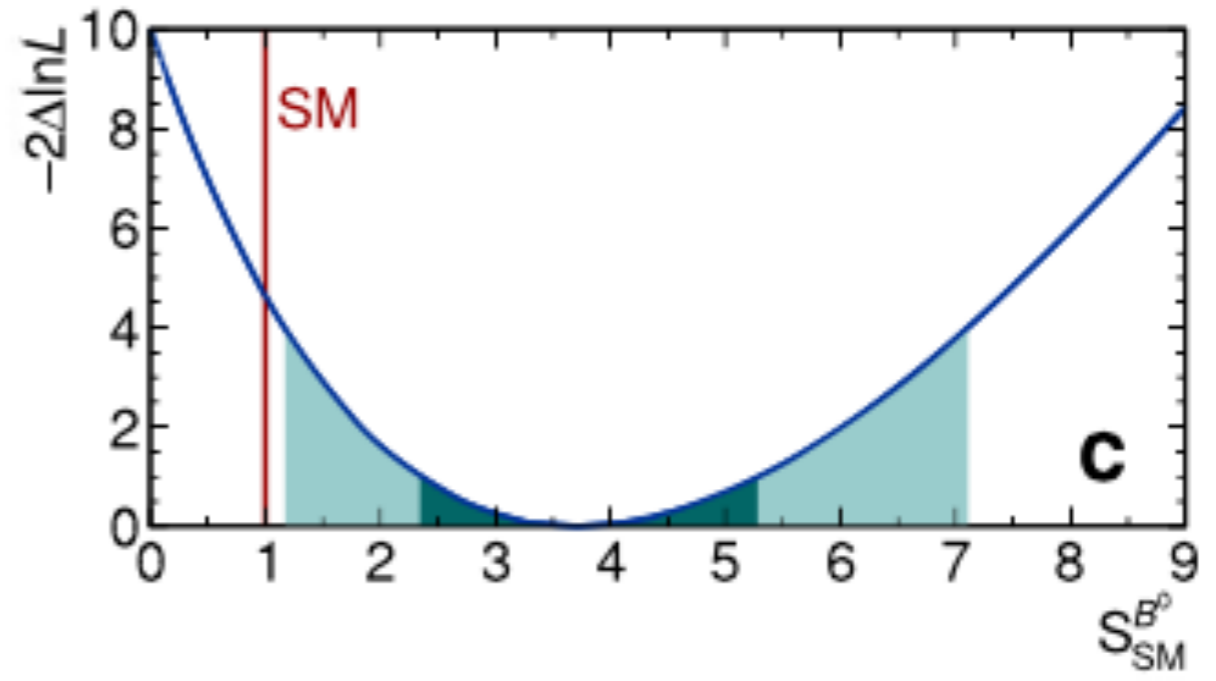
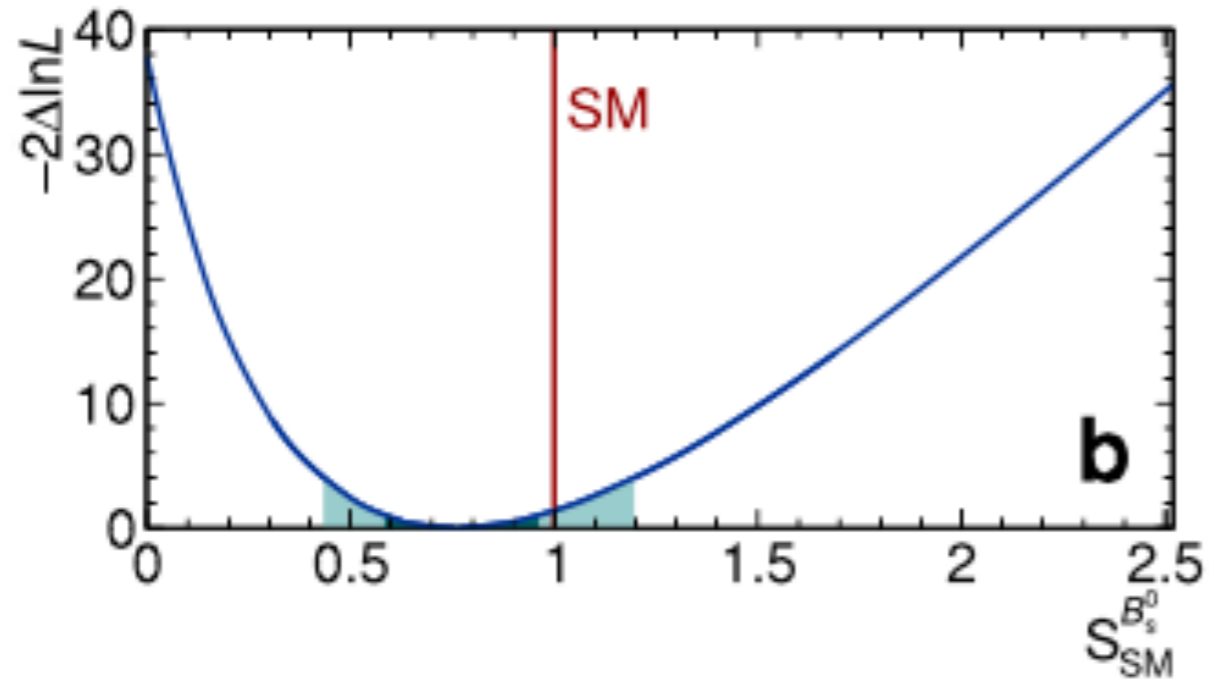
CMS+LHCb II

- ◆ 2D contour plot of branching ratios
 - B_s too small by 1σ
 - B too big by $\approx 2\sigma$



CMS+LHCb II

◆ Individual contour plots

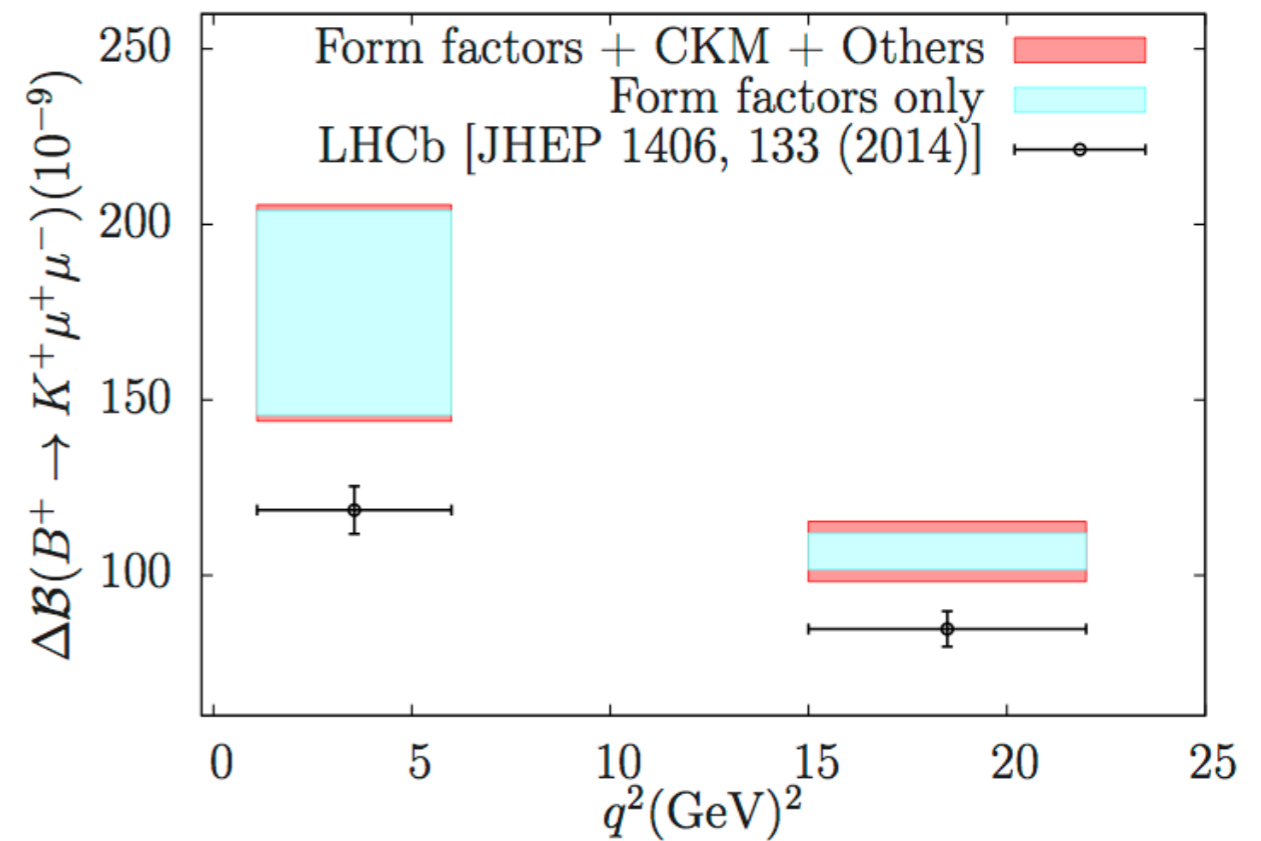
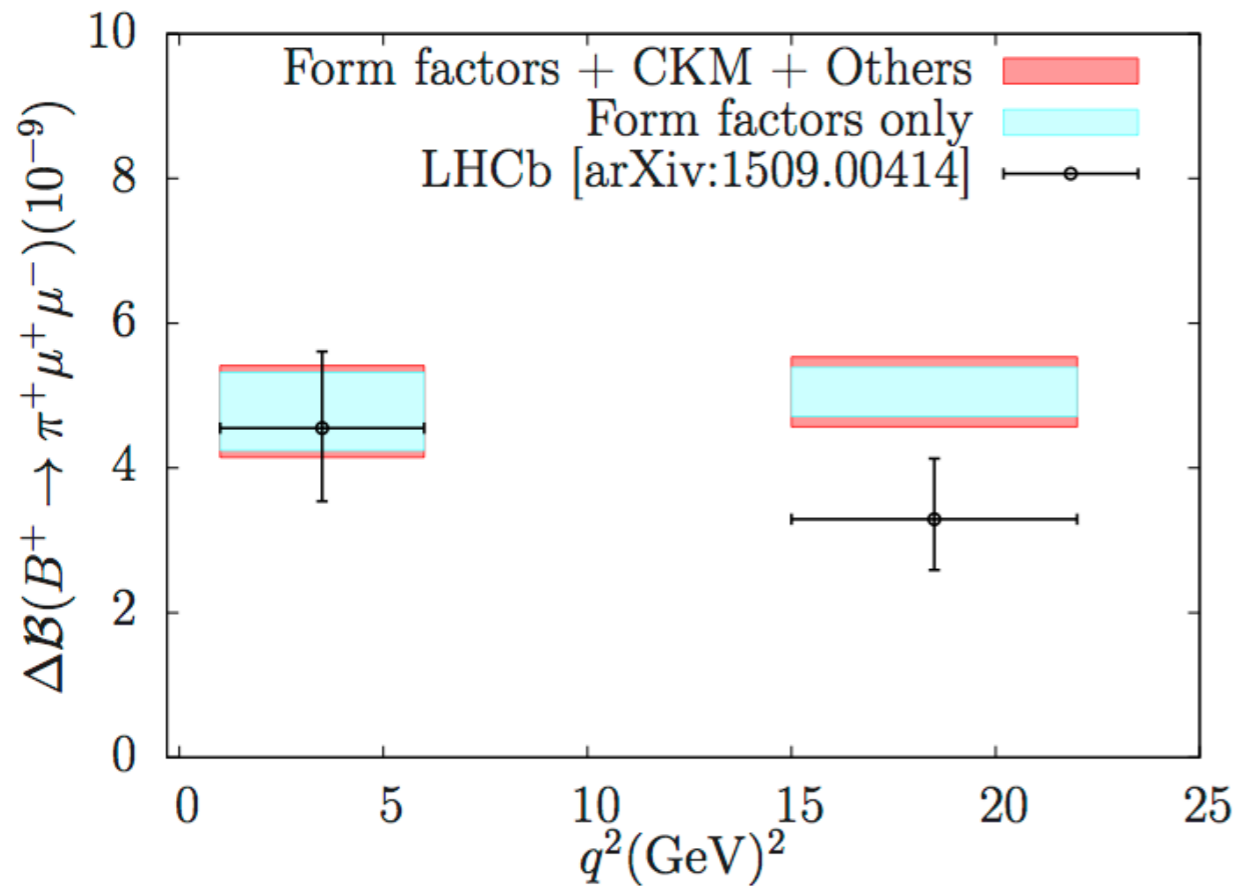


Rare B Decays



- ◆ FNAL/MILC has recently calculated form factors needed for several rare decays that require flavor changing neutral current.
- ◆ Good place to look for new physics
- ◆ Some tension between SM prediction and recent LHCb measurement

Rare B Decays II



- LHCb measurement is smaller than SM prediction in 3 of 4 bins. 1.7σ tension.
- arXiv:1510.02349

Rare B Decays III

- ◆ Rare decays depend on $|V_{tq}|$ with $q=d$ or s

$$|V_{td}| = 7.45(69) \times 10^{-3}, \quad |V_{ts}| = 35.7(1.5) \times 10^{-3}$$

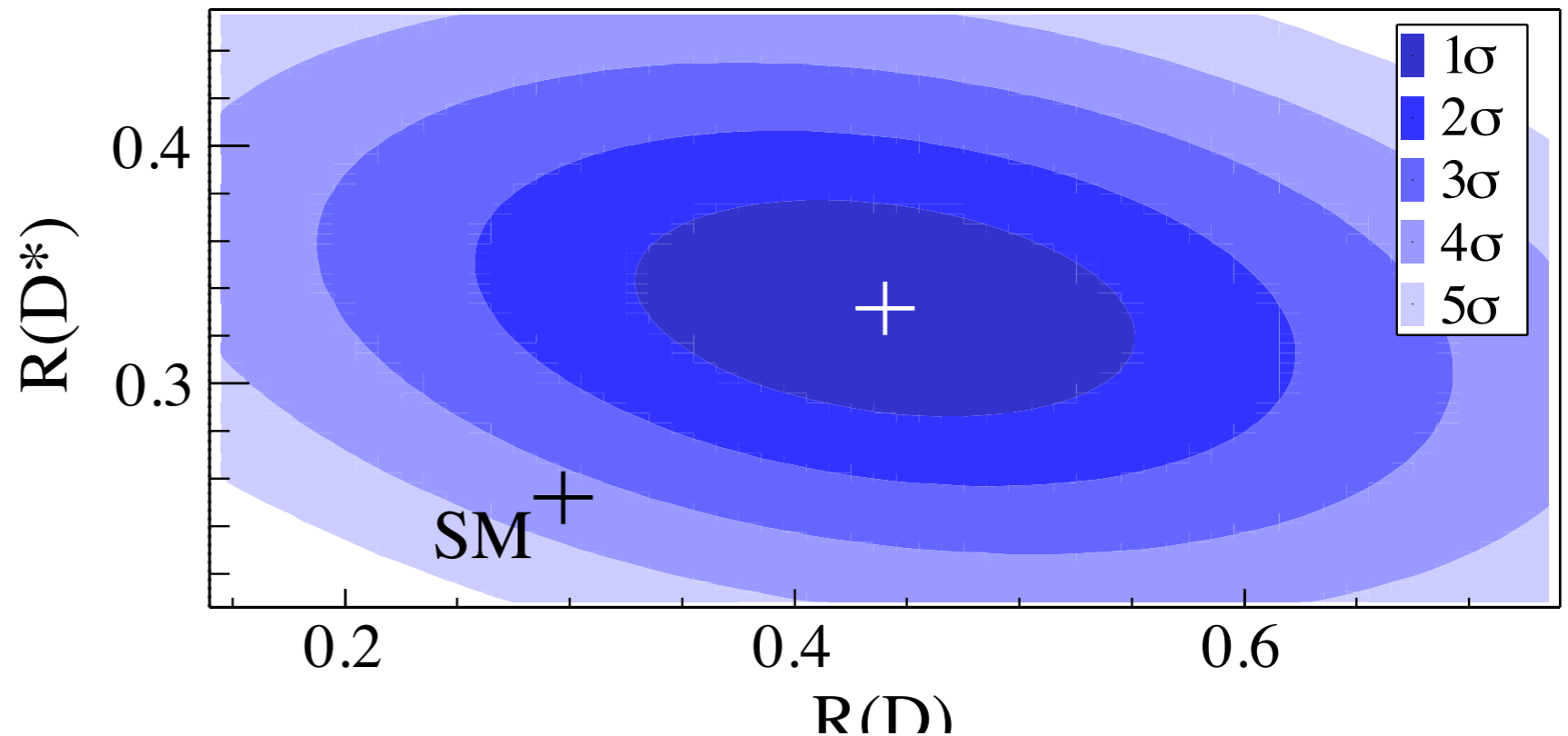
- ◆ The same elements of CKM matrix can be determined from B-meson mixing

$$|V_{td}| = 8.4(6) \times 10^{-3}, \quad |V_{ts}| = 40.0(2.7) \times 10^{-3}$$

- ◆ New $|V_{ts}|$ is 1.4σ below that from mixing with smaller error
- ◆ Values of $|V_{td}|$ are comparable
- ◆ LQCD will help improve both determinations

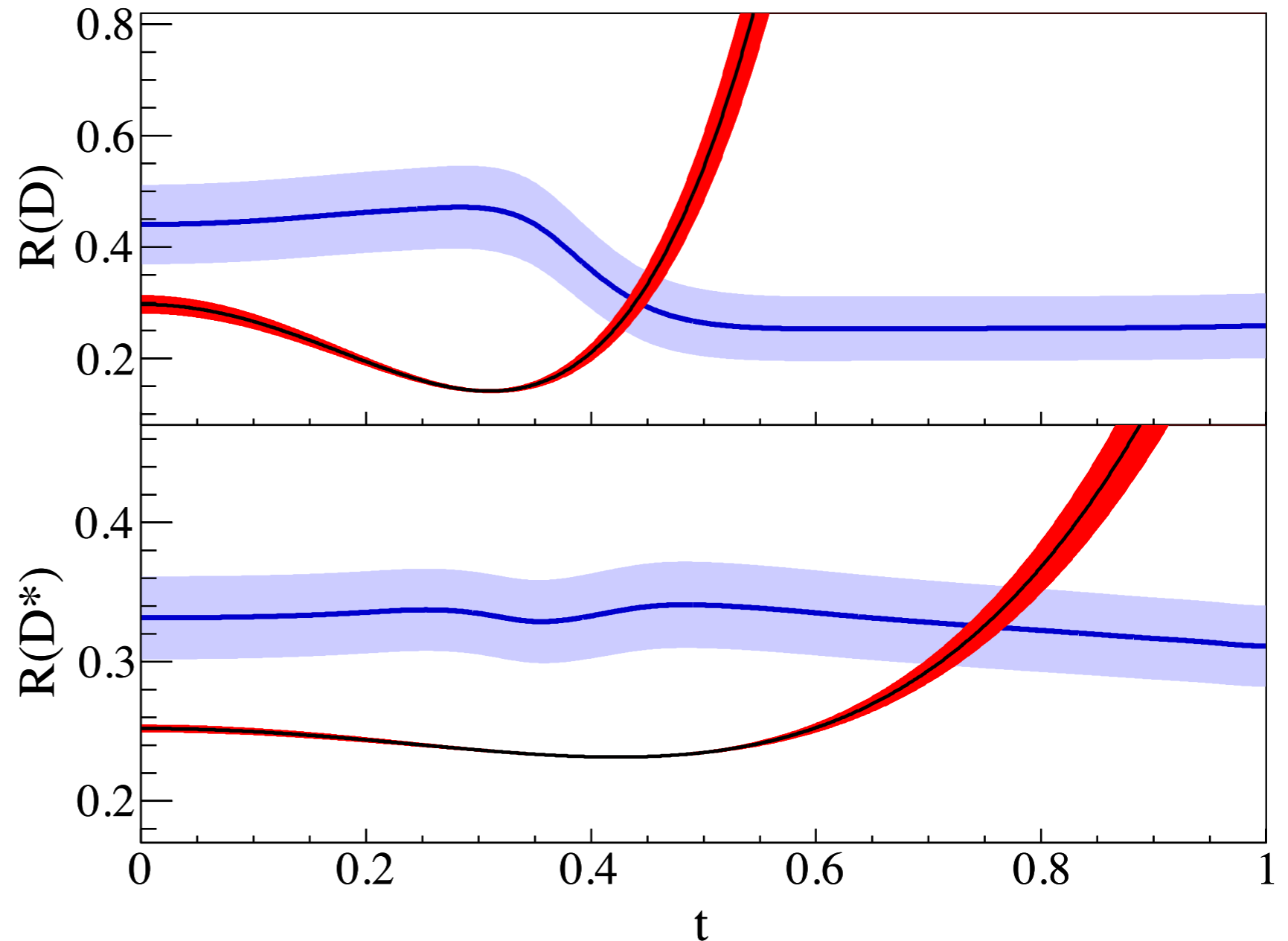
R(D) and R(D*)

- BaBar: PRD88, 072012 (2013)
- FNAL/MILC: PRL109, 071802, (2012)
- R(D): 2.0σ
- R(D*): 2.7σ
- Together: 3.4σ
- all BaBar's values
- However, no agreement is 2H model

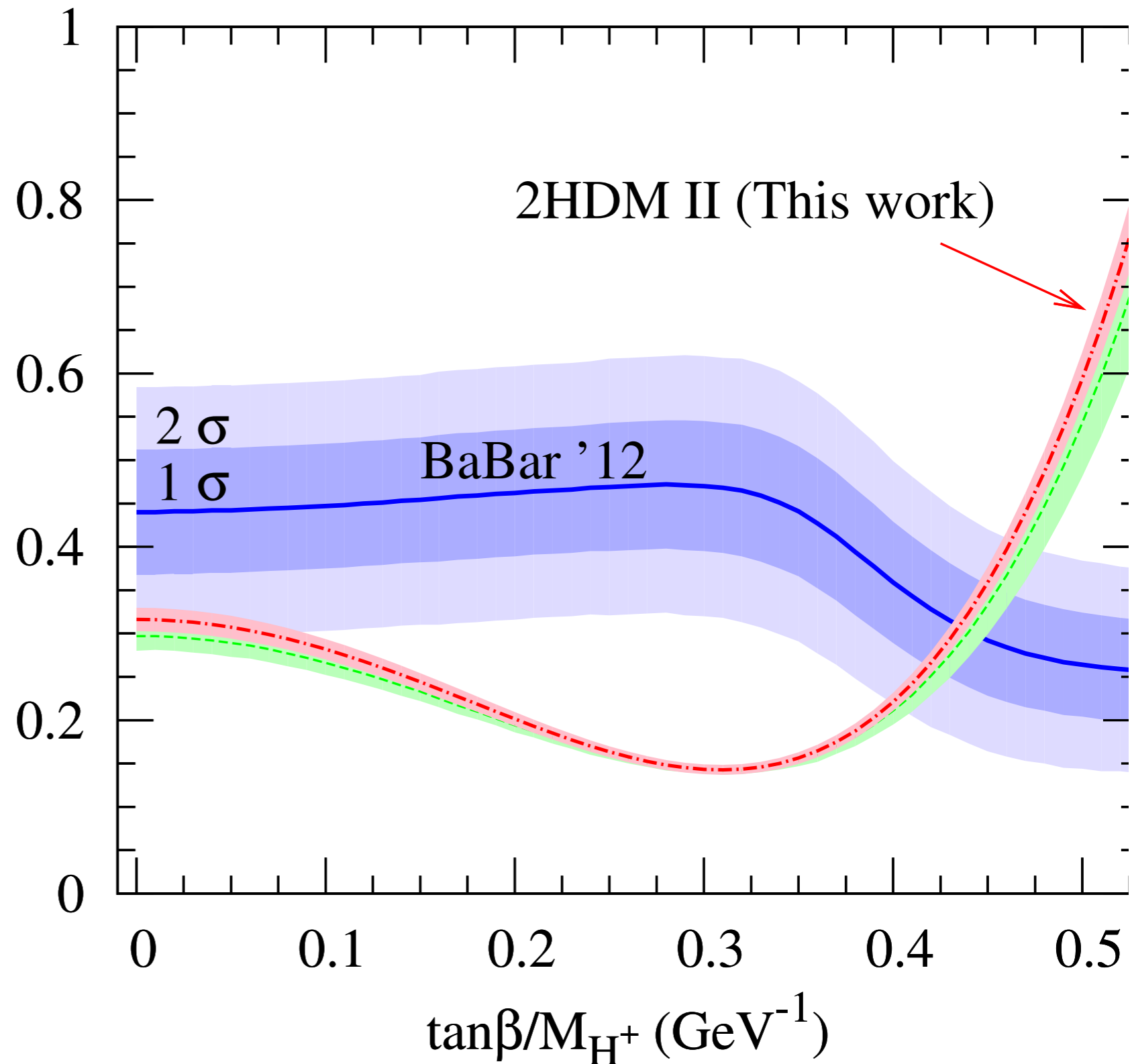


R(D) and R(D*) II

- BaBar's comparison with two Higgs doublet model predictions
- x-axis should be $\tan(\beta)/M_H$



- We slightly improve agreement between BaBar result and standard model.



Introduction

- ◆ Goal is quick summary of some of the places where there is a hint of beyond the standard model physics.
 - Emphasis on where lattice QCD might have an impact.
 - Many graphs from our recent papers.
- ◆ Obvious non-lattice:
 - neutrino masses and mixing
 - dark matter
 - dark energy
- ◆ Muon $g-2$
 - Many talks on this subject, so just point out it is one of the most significant anomalies.